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## PAPER

## Single-electron thermal devices coupled to a mesoscopic gate

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**Abstract**

We theoretically investigate the propagation of heat currents in a three-terminal quantum dot engine. Electron–electron interactions introduce state-dependent processes which can be resolved by energy-dependent tunneling rates. We identify the relevant transitions which define the operation of the system as a thermal transistor or a thermal diode. In the former case, thermal-induced charge fluctuations in the gate dot modify the thermal currents in the conductor with suppressed heat injection, resulting in huge amplification factors and the possible gating with arbitrarily low energy cost. In the latter case, enhanced correlations of the state-selective tunneling transitions redistribute heat flows giving high rectification coefficients and the unexpected cooling of one conductor terminal by heating the other one. We propose quantum dot arrays as a possible way to achieve the extreme tunneling asymmetries required for the different operations.

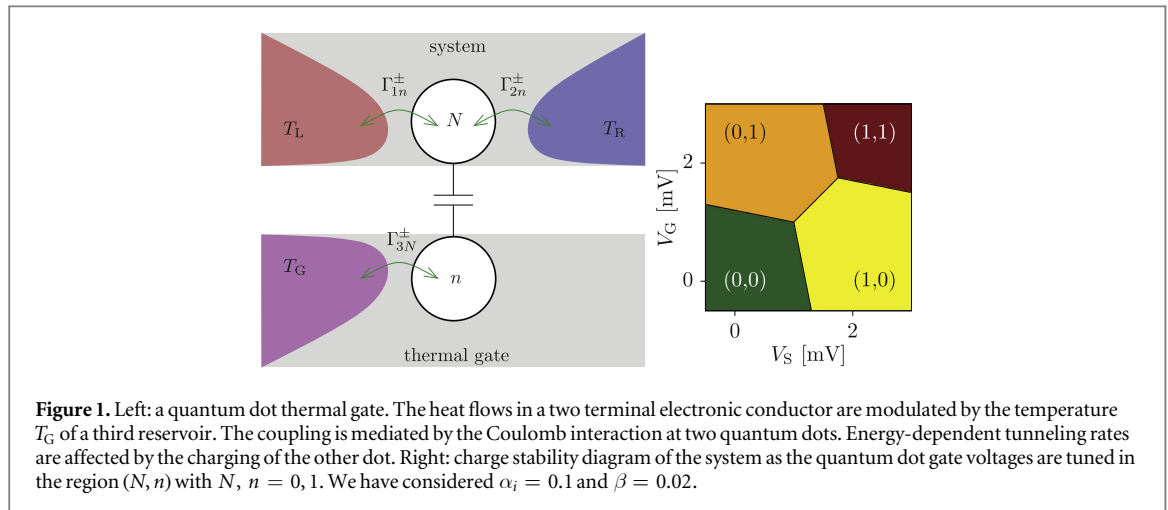
**1. Introduction**

The control of heat flows in electronic conductors is one of the present day technological challenges. Besides the conversion of heat currents into electrical power which is the main focus of thermoelectrics, there is the possibility of making all-thermal circuits that work only with heat currents and temperature gradients. For this purpose, all-thermal versions of electronic devices such as diodes and transistors need to be operative.

Mesoscopic conductors are good candidates [1, 2]: their energy spectrum can be easily designed by using low dimensional structures showing quantum confinement (quantum dots, quantum wires...). Also, the presence of different gaps due to interaction effects (e.g. Coulomb blockade) or superconductor interfaces can be controlled. This possibility has been evident in the last years with the proposal and experimental realization of heat engines [3–17] and electronic refrigerators [1, 18–24] based on nanoscale systems, and with the detection of heat currents [18, 25–29]. Thermal rectifiers and transistors have also been proposed [30–43] and experimentally implemented [44–47].

A crucial aspect for an electronic thermal device is how it interacts with its environment. Inelastic transitions in the device can be due to the coupling to fluctuations in the electromagnetic environment [43, 48, 49], or to phononic [50, 51] or magnetic [52] baths. Remarkably in mesoscopic conductors, the dominant interaction can be engineered by introducing additional components which mediate the coupling to the environment, e.g. a quantum point contact [53], quantum dots [11, 12, 54], or photonic cavities [55–57]. This allows one to define different interfaces for the different operations. From a theoretical point of view, this permits the environment to be described as a third terminal, and the auxiliary system (mediating the system–environment coupling) to be treated in equal footing as the conductor.

Here we propose a multi-terminal system of two capacitively coupled quantum dots as a versatile configuration for the efficient manipulation of electronic heat currents, as sketched in figure 1. It works as a bipartite system: one of them is coupled to two terminals and is considered as the conductor whose heat currents are to be manipulated. The other dot is tunnel-coupled to a third terminal and serves as a gate system. Energy exchange between the two systems is mediated by electron–electron interactions [58–62]. Effects such as mesoscopic Coulomb drag [63–66], enhanced correlations [67–70], heat engines [11–14, 71–74], rectification of



noise [54, 75], non-local power generation [76], relaxation time scales [77], or the relation of information and thermodynamics [78–80] have been investigated in similar configurations. Thermoelectric effects in three terminal configurations have been described where the coupling of a junction to the heat source is mediated by other kinds of interactions [15, 48–53, 57].

Energy exchange mediated by electrostatic coupling has the additional advantage of allowing for defining thermal insulating system-gate interfaces. This way eventual heat currents leaking from the gate to the conductor, e.g. due to phonons, are suppressed. Also, phononic heat currents along the conductor are not affected by charge fluctuations in the gate and hence are not expected to affect the thermal gating effects. Furthermore, in the low temperature regime discussed here, the contribution of phonons in the conductor can be neglected.

In a recent experiment [81], the gating of voltage-induced electronic currents in the conductor by the modulation of the temperature of the gate was observed. We extend the investigation of such thermal gating to the gating of thermally-induced heat currents. A first step was done in [82] where the gate dot acts as a switch. As we show here, exploiting the energy dependence of tunneling effects in the conductor dot, the same device becomes a versatile thermal device. We connect the different operations of the device to different asymmetries. Energy-filtered couplings lead to a thermal transistor (section 4). Combined energy-dependent and left–right asymmetries give a thermal diode as well as the effect of cooling by heating (section 5). We discuss possible implementations of all these asymmetries and how to tune them with quantum dot arrays in section 6.

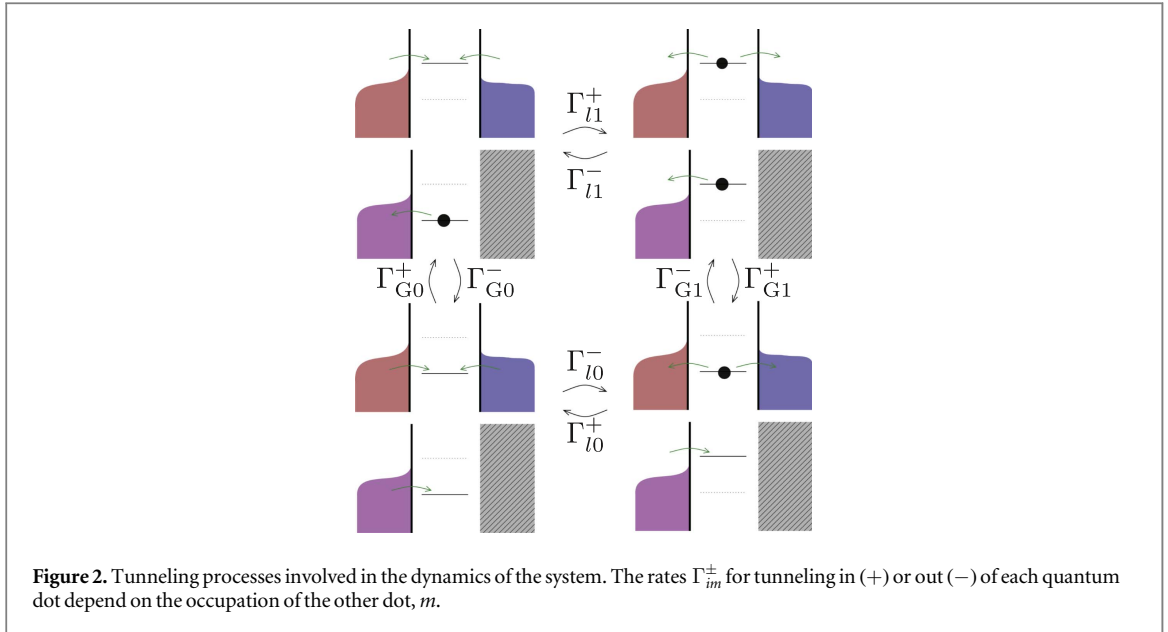
In the remaining of the text, section 2 describes the theoretical model and the heat currents and section 3 introduces the thermal gating effect. Conclusions are discussed in section 7.

## 2. Heat currents

Our model is based on the interaction of two mesoscopic systems: the conductor system and the thermal gate. For capacitively coupled quantum dots, the interaction is given in terms of the electrostatic repulsion of electrons occupying them. For simplicity, we will assume that it is very large for electrons in the same dot, so we restrict our considerations to single-electron occupations in each quantum dot. Interdot Coulomb interaction is described by a constant  $E_C$  given by the geometric capacitances of the system [11].

Through all this work, we consider non-equilibrium situations only due to temperature gradients  $\Delta T_i = T_i - T$  applied to one terminal with respect to the reference temperature,  $T$ . We do not restrict to the linear regime where gradients are small. No bias voltage is applied. Index  $l = L, R$  will always refer to the conductor terminals, while  $i$  labels any terminal.  $G$  will denote the gate. The internal potential  $U_{im}$  of each quantum dot  $i$  is then shifted by  $E_C$  when the charge of the other dot  $m$  fluctuates:  $U_{i1} = U_{i0} + E_C$ . Hence every energy exchange between the system and the gate is given in terms of this quantity.

In an experimental realization, the internal potentials are tuned by means of gate voltages which we include with their corresponding lever arms  $\alpha_i$  and  $\beta$ :  $U_{S0} = \varepsilon_S + \alpha_S e V_S + \beta e V_G$ , and  $U_{G0} = \varepsilon_G + \alpha_S e V_S + \beta e V_G$ . This way, the charge configuration of the system can be externally manipulated by moving  $U_{im}$  with respect to the Fermi energy of the leads,  $\mu_i$ . This is shown in figure 1: each region of this stability diagram is dominated by one of the occupations  $(N, n)$ , with  $N, n = 0, 1$ , where  $N$  represents the occupation of the system and  $n$  denotes the occupation of the gate. Charge fluctuates around the intermediate regions.



Two triple points appear where charge fluctuations are present in both dots. We call the region between them the stability vertex, whose size is given by  $E_C$ . Thermoelectric heat engines based on the correlation of the system and the gate operate in this region [11, 12, 80].

We write a rate equation for the occupation of the charge states  $\lambda = (N, n)$ :

$$\dot{P}(\lambda) = \sum_{\lambda'} [\Gamma_{\lambda \leftarrow \lambda'} P(\lambda') - \Gamma_{\lambda' \leftarrow \lambda} P(\lambda)], \quad (1)$$

with the tunneling rates  $\Gamma_{(1,n) \leftarrow (0,n)} = \sum_l \Gamma_{ln}^+$  (with  $l = L, R$ ), and  $\Gamma_{(N,1) \leftarrow (N,0)} = \Gamma_{GN}^+$ . For the reversed processes, we replace  $+\rightarrow-$ . They are written as  $\Gamma_{im}^{\pm} = \Gamma_{im} f_i^{\pm}(\Delta U_{im})$ , where the transparencies of the barrier  $\Gamma_{im}$  depend on the occupation  $m$  of the other dot,  $f_i^+(E) = [1 + e^{E/k_B T}]^{-1}$  is the Fermi function, and  $f_i^-(E) = 1 - f_i^+(E)$ . We have defined  $\Delta U_{im} = U_{im} - \mu_i$ . We assume weak dot-lead couplings,  $\Gamma_{im} \ll k_B T$ , where transport is dominated by sequential tunneling events. A schematic representation of the possible trajectories is represented in figure 2.

The dc heat currents are obtained by the steady state occupations  $\bar{P}(\lambda)$  satisfying:  $\dot{\bar{P}}(\lambda) = 0$ . They are given by [11]:

$$J_l = \sum_n \Delta U_{ln} [\Gamma_{ln}^+ \bar{P}(0, n) - \Gamma_{ln}^- \bar{P}(1, n)], \quad (2)$$

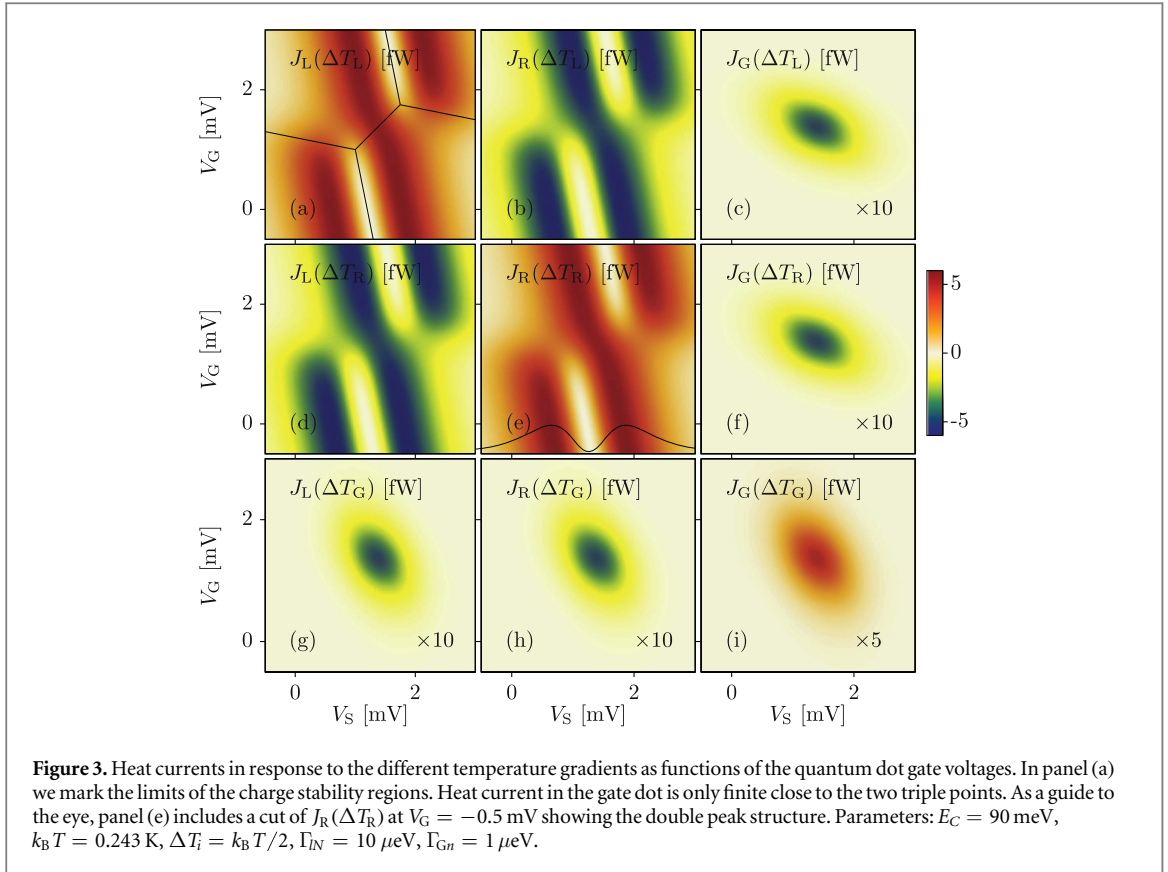
$$J_G = \sum_N \Delta U_{GN} [\Gamma_{GN}^+ \bar{P}(N, 0) - \Gamma_{GN}^- \bar{P}(N, 1)]. \quad (3)$$

They are defined as positive when heat flows out the terminal. From the previous expressions, one can straightforwardly write the state-resolved currents  $J_{ln}$  and  $J_{GN}$  such that:  $J_i = \sum_m J_{im}$  [71]. As we are applying no bias voltage, heat is conserved, and  $\sum_i J_i = 0$ . In the following, we write  $J_i(\Delta T_j)$  as the heat current injected from terminal  $i$  in response to a temperature gradient applied to terminal  $j$ , with all other terminals being (except when explicitly stated) at temperature  $T$ .

The discrete level of the quantum dots filters the energy of the tunneling processes. The flow of heat is restricted to the region where they are close to the Fermi energy, as shown in figure 3. When the temperature gradient is applied longitudinally in the conductor (i.e. either in the left or right terminal), the conductor heat currents present a double peak around the crossing of the level with the Fermi energy. At that particular point far from the stability vertex (such that fluctuations in the gate are frozen),  $J_l = 0$  because of particle-hole symmetry. This is a well-known feature of two-terminal quantum dots [83]. In our system, such a signal is broken at the stability vertex as a consequence of the charging of the gate dot.

The mechanism for heat transport in the gate is different. It relies on charge fluctuations in the two dots which involve the four charging states in a closed loop trajectory [11]. In a sequence of the form  $(0, 0) \leftrightarrow (1, 0) \leftrightarrow (1, 1) \leftrightarrow (0, 1) \leftrightarrow (0, 0)$ , the events of tunneling in and out of the gate dot occur at different energies due to the different occupations of the conductor dot. The energy difference,  $\pm E_C$ , is transferred between the two-terminal conductor and the gate. The sign of the transfer depends on the direction of the above sequence. Hence  $J_G(\Delta T_j)$  shows up as a spot in the middle of the stability vertex [80], as shown in figure 3.

In agreement with the Clausius statement of the second law, heat flows out of the hot reservoirs, as shown in the diagonal panels, starting from the top left, in figure 3. We note that in the symmetric configuration shown



there, the absorption of this heat current is shared by the corresponding other (cold) terminals, where currents are negative. As we discuss below, this is not necessarily the case in the presence of energy-dependent rates.

### 3. Thermal gating

The effect of the gate dot on the heat flow in the conductor is twofold: it exchanges heat with the conductor and affects the heat flow *within* the conductor. The former one modifies energy conservation. The second is due to the shift in the position of the energy level of the conductor when the occupation of the gate dot changes. This breaks the double peak structure shown in figure 3. The effect is evident in the stability vertex where transport fluctuations in the conductor coincide with charge fluctuations in the gate dot [70]. These occur at a higher rate when the gate reservoir is hot. Hence tuning the temperature  $T_G$  modifies the transport properties of the conductor. We call this the thermal gating effect.

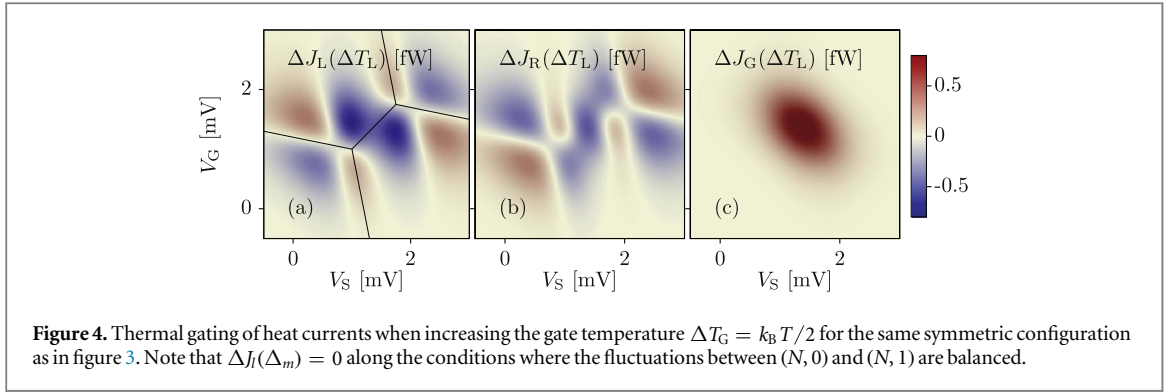
In the electric response, it manifests as a clover-leaf structure with positive and negative regions around the stability vertex [81, 84]. The sign can be understood in terms of dynamical channel blockade: it depends on whether the fluctuations in the gate dot contributes to open or close the relevant transport channels [58, 59, 67, 69, 85].

Here we are interested in the thermal gating of heat currents. We quantify it by defining the modulation:

$$\Delta J_i(\Delta T_j) = J_i(\Delta T_j, \Delta T_G) - J_i(\Delta T_j, 0). \quad (4)$$

We plot it in figure 4 for a symmetrical configuration with  $\Gamma_m = \Gamma$ . For heat currents, we observe a clover-leaf structure centered at each triple point. Interestingly,  $\Delta J_i = 0$  along the conditions  $P(N, 0) = P(N, 1)$ . There, the level of the gate dot is aligned with the Fermi energy such that charging/uncharging the gate dot is independent of the lead temperature.

The clover-leaf structures are the effect of thermal gating due to fluctuations in the gate. However, in the center of the stability vertex we also observe signatures of the additional effect of energy exchange with the gate system. Obviously, if we inject heat from a third terminal, the total heat flow in the conductor is affected. The performance of our system as an all-thermal device, e.g. a thermal transistor, requires the suppression of such contributions. For example, reducing the transparency  $\Gamma_{GN}$  reduces  $J_G$ , leaving the clover leaf structure almost unaffected [84]. This is an indication that based on fluctuations of the gate only one can have a thermal gating effect, in principle involving no heat injection into the conductor.



#### 4. Energy filtering: a thermal transistor

An all-thermal transistor modifies the heat current in a conductor due to changes in the temperature of a third (gate) terminal. This is the thermal gating effect discussed in the previous section. In this case, the two conductor terminals act as the emitter and the collector, while the gate terminal is considered as the base. As for an electric transistor, we can define the thermal amplification factor as [39, 42]:

$$\alpha_{tm} = \frac{|\Delta J_l(\Delta T_m)|}{|\Delta J_G(\Delta T_m)|}, \quad (5)$$

where  $\Delta J_G(\Delta T_m)$  is the change of heat injected from the gate when tuning  $T_G$ . For the system to work as a thermal transistor, one needs  $\alpha_{tm} \gg 1$ .

The challenge is to achieve a measurable thermal gating by injecting a small amount of heat from the gate. In our system, heat is injected only via electron–electron interactions and we can therefore control it by selecting the charge of the system. As discussed above, the mechanism for heat transfer in our system is based on the occurrence of charge fluctuations involving all the four charging states in a loop, as presented in figure 2. In this section we discuss how to avoid such trajectories. We will see that this is the most effective way to suppress the energy exchange between the system and the gate, while still having a gating effect. This can be achieved either by operating at low temperature,  $kT \ll E_C$  (i.e. eliminating one of the states), or by acting on the energy-resolved tunneling rates (eliminating one of the transitions) [82]. Time-resolved measurement of fluctuations in the former configuration have been recently reported in single-electron transistors [86].

We focus here on the second case, where the tunneling rates in the conductor are strongly energy dependent, for instance  $\Gamma_0 \ll \Gamma_1$ . This allows us to consider the regime  $k_B T \sim E_C$ . An energy dependence in tunneling rates is expected to occur naturally as in quantum mechanics the tunneling probability depends exponentially on the energy of the electron with respect to the height of the barrier. Furthermore, in semiconductor quantum dots, the energy dependence of the barrier transparencies can be modulated experimentally by means of gate voltages [12]. Additionally, a more complicated quantum dot composition can be used, where only two dots provide the system-gate interface and the other ones are used as energy filters. We discuss several such geometries in section 6.

In the limit  $\Gamma_0 = 0$ , the transitions  $(0, 0) \leftrightarrow (1, 0)$  are avoided. Hence the state  $(1, 0)$  is only populated through fluctuations of the form  $(1, 1) \leftrightarrow (1, 0)$  taking place in the gate dot. Currents in the conductor are conditioned on the occupation of the gate dot. When it is empty, the transport transitions are blocked. We can then write:  $J_l = J_{l1}$  and  $J_{l0} = 0$ . The gate dot becomes a switch.

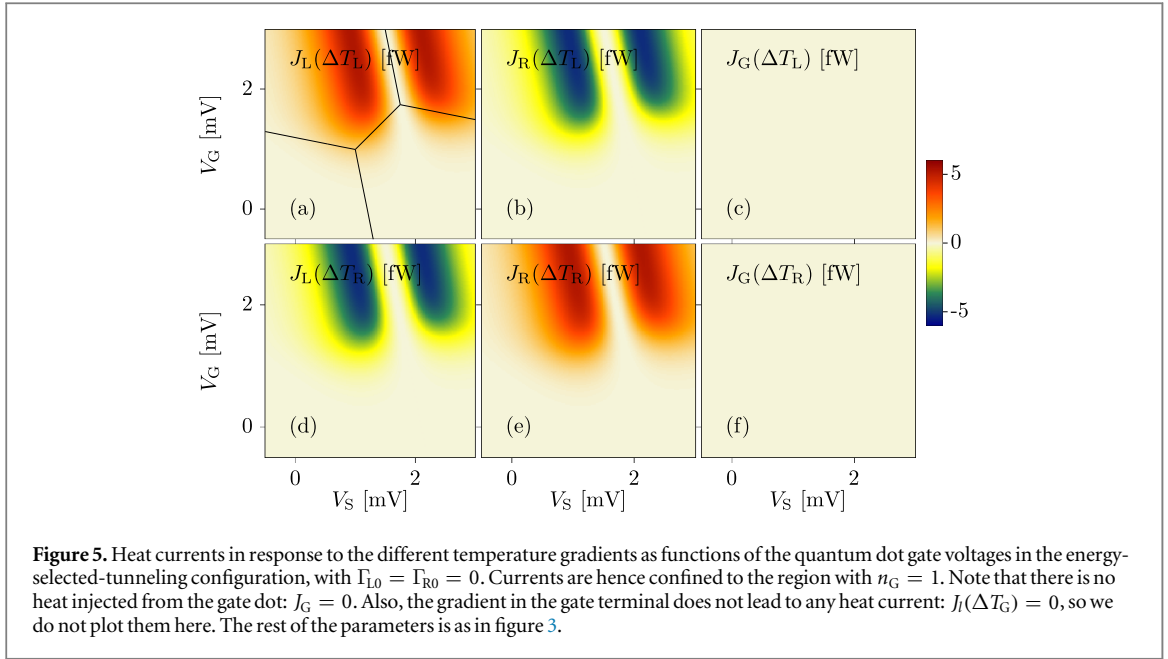
In this case, there are no transitions that correlate fluctuations at the two dots. Then, state-dependent currents are conserved in each conductor:  $J_{l0} = 0$ ,  $J_{l1} + J_{r1} = 0$ , and  $J_{GN} = 0$  [71]. From the latest and equation (3), we get the relations:

$$\bar{P}(N, 0) = e^{\Delta U_{GN}/k_B T_G} \bar{P}(N, 1), \quad (6)$$

emphasizing that the gate satisfies detailed balance. Using the level-resolved conservation laws given above, this model admits a simple analytical solution without needing to solve the master equation. The heat currents in the conductor are:

$$J_l = \Delta U_l \Gamma_{\text{seq}l} (f_{l1} - f_{\bar{l}1}) \langle n(T_G) \rangle, \quad (7)$$

where we have written  $\Gamma_{\text{seq}l}^{-1} = \sum_l \Gamma_{l1}^{-1}$ ,  $f_{l1} = f_l(\Delta U_{l1})$ , and  $\bar{l}$  is the opposite terminal to  $l$  in the conductor. The effect of the gate enters only in the average occupation  $\langle n(T_G) \rangle = P(0, 1) + P(1, 1)$  given by:



$$\langle n(T_G) \rangle = \frac{\sum_i \Gamma_{ih} f_{G0} f_{G1}}{\sum_i (\Gamma_{ih}^+ f_{G0} + \Gamma_{ih}^- f_{G1})}. \quad (8)$$

It modifies the current expected for an isolated single channel at energy  $\varepsilon$ :

$$J_{sc,i}(\varepsilon) = \varepsilon \Gamma_{seq}(\varepsilon) [f_i(\varepsilon - \mu) - f_{\bar{i}}(\varepsilon - \mu)]. \quad (9)$$

This effect can be clearly observed in figure 5, where all possible currents in response to a temperature gradient applied to the different terminals of the conductor are plotted. By comparing it with the symmetric (energy independent) rates configuration shown in figure 3, we observe that transport is suppressed in the lower region of the stability diagram, where  $\langle n \rangle \approx 0$  as a result of the asymmetric tunneling rates.

We note that no heat current flows from the gate into the conductor. Nevertheless, the thermal gating effect exists (see figure 6) due to the dynamical blockade of the heat currents:

$$\Delta J_i(\Delta T_m) = J_{sc,i}(\Delta U_{ih}) [\langle n(T_G + \Delta T_G) \rangle - \langle n(T_G) \rangle]. \quad (10)$$

In this case only the clover-leaf around the triple point close to (1, 1) appears. Also,  $J_G = 0$  for any configuration, as expected, and  $\Delta J_G(\Delta T_L) = 0$ . As a consequence, the thermal amplification factor diverges (within our approximations) and the system operates as an ideal transistor. Note that the leading order in an expansion of the thermal gating for this case is quadratic in the temperature gradient:  $\Delta J_i(\Delta T_j) \sim \Delta T_j \Delta T_G$ .

#### 4.1. Leakage currents

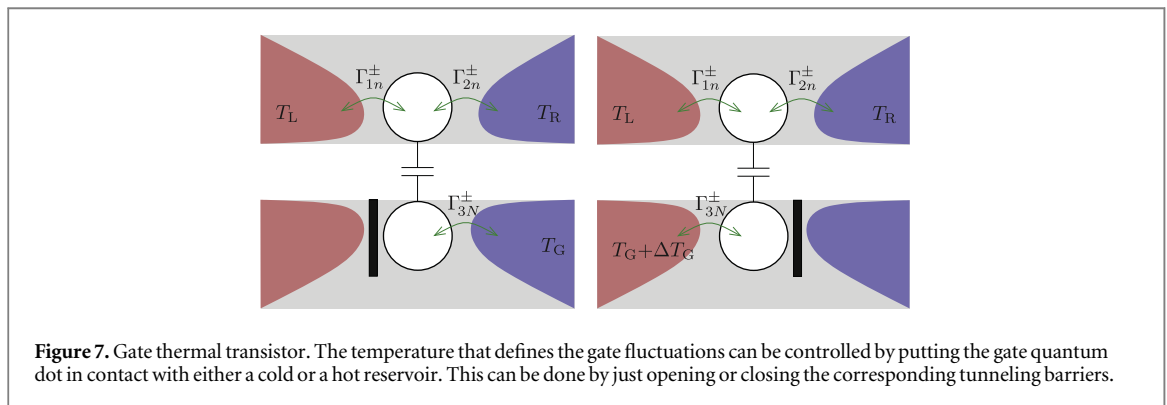
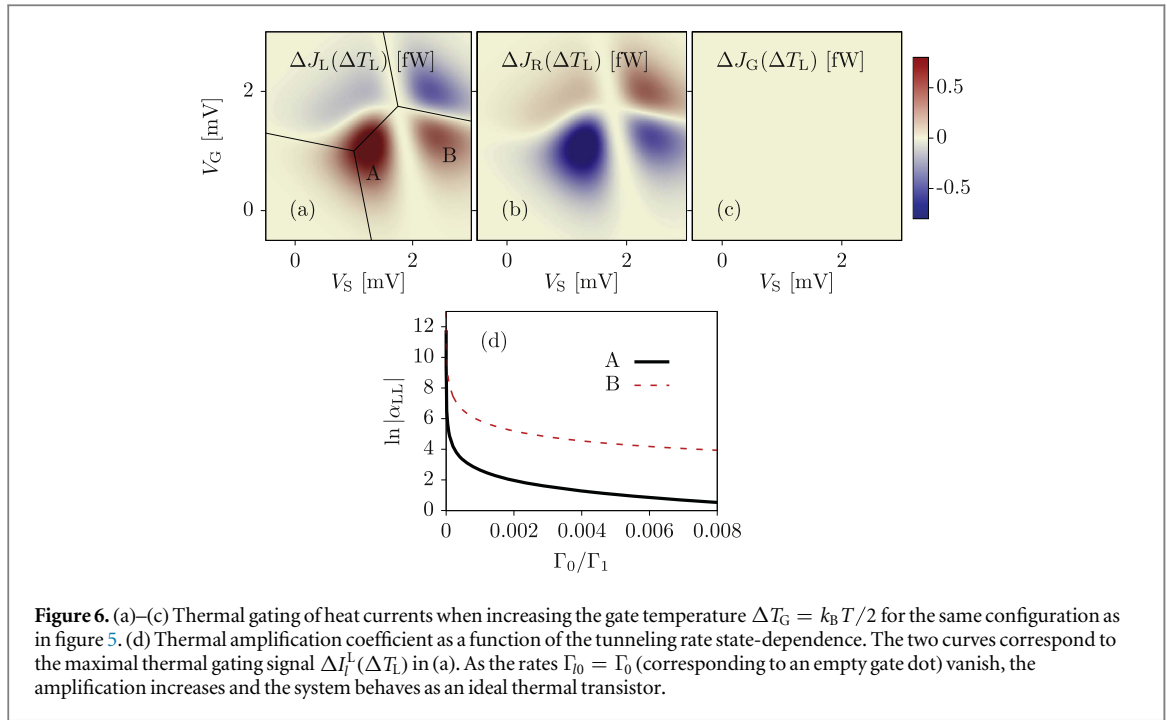
Of course, in a real setup the transition rates cannot be exactly suppressed. In that case, heat leaks from the gate and the amplification coefficient becomes finite. We take this into account in figure 6, where  $\alpha_{LL}$  is calculated at the two maxima of  $\Delta J_L(\Delta T_L)$  (labeled as A and B in figure 6(a)) for finite values of  $\Gamma_{l0} = \Gamma_0$ . For  $\Gamma_0 < \Gamma_1/100$ , the amplification factor is several orders of magnitude larger than 1. Note that in the presence of a leakage current, the maximum at B (which is further from the stability vertex and is hence less affected by the leakage) gives a larger amplification factor, even if  $\Delta J_L(\Delta T_L)|_A > \Delta J_L(\Delta T_L)|_B$  for  $\Gamma_0 = 0$ .

Being closer to the relevant triple point where sequential tunneling transitions are dominant, B is also expected to be less sensitive to higher-order tunneling processes (neglected here). These involve energy transfer between the two systems and hence avoid the divergence also in the ideal case  $\Gamma_{l0} = 0$ .

#### 4.2. Thermal gating without heating

As we discuss above, a thermal transistor can work without any injection of heat in the conductor. This does not necessarily mean that it works without any energy cost: in order to increase  $T_G$  one in principle has to inject heat into the gate terminal.

In this respect, single-level quantum dots are also beneficial: the state of the dots is highly non-thermal and no temperature of the dot can be defined [76]. The dynamics of the system depends on the non-equilibrium charge fluctuations in the quantum dots. The relevant gate temperature is that of the reservoir to which the quantum dot is coupled. We can then think of a configuration such that the gate dot is tunnel-coupled to two



terminals, one cold and one hot, as depicted in figure 7. By alternatively opening and closing one of the barriers, the charge fluctuations will adapt to the temperature of only one of them. Increasing  $\Delta T_G$  can then be done at an arbitrarily low energy cost (that of tuning the gates that control the barriers).

Furthermore, the cold and hot reservoirs in the gate can even be in thermal contact with the conductor terminals. This way, only one thermal gradient is needed: the one that drives the heat currents in the conductor. The system is then reduced to two terminals connected in parallel by two interacting quantum dots: one supports a heat current. The other one is put in contact with only one of the reservoirs at a time. The current thus depends on to which side the gate dot is coupled.

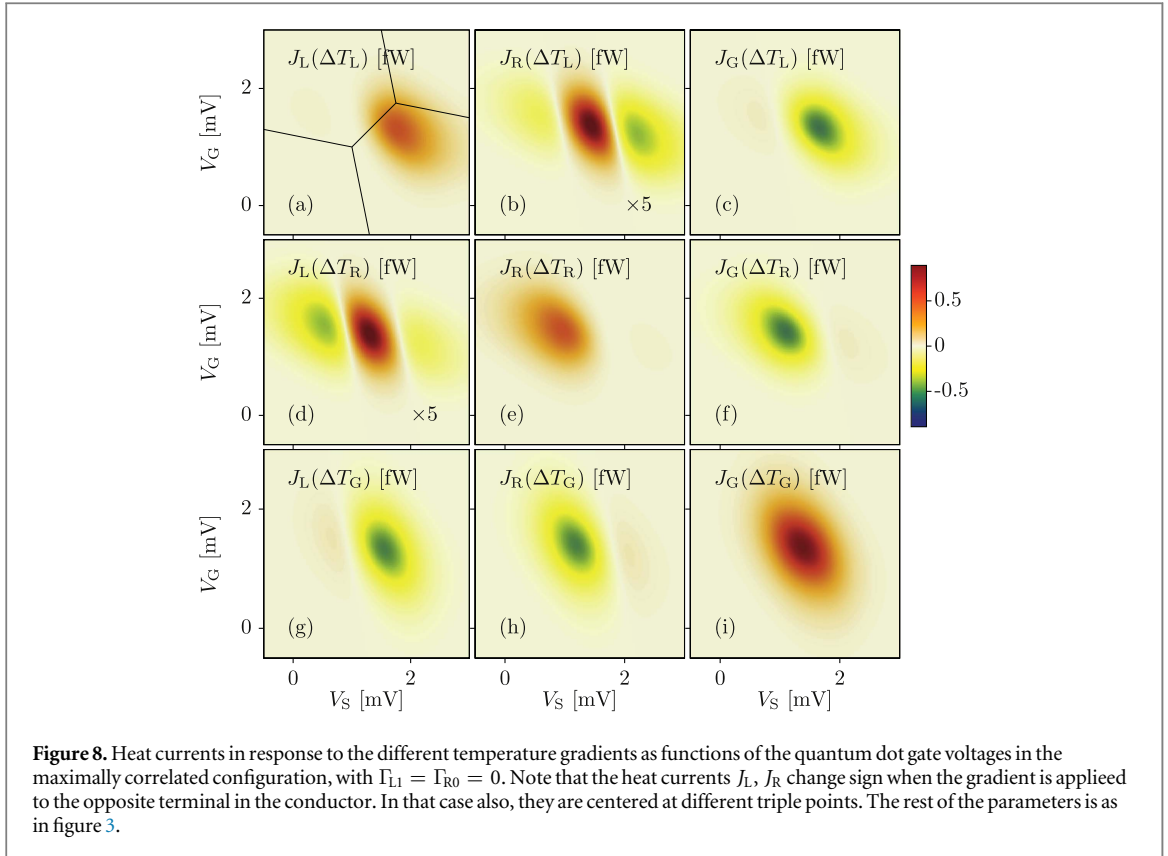
## 5. Combined state-dependent and mirror asymmetric tunneling: thermal rectification

The energy-dependent tunneling rates introduced by the coupling to the gate dot may also generate left–right asymmetries in the propagation of heat in the conductor: the energy at which electrons will more probably tunnel through the two barriers will be different. Transport would then depend on where the temperature gradient is applied, leading to a thermal rectification effect, if  $J_L(\Delta T_R) \neq J_R(\Delta T_L)$ .

A conductor that exploits this property by allowing the heat to flow for a forward, but not for a backward gradient is a thermal diode. It is characterized by the thermal rectification coefficient, defined as:

$$\mathcal{R} = \frac{|J_L(\Delta T_R) - J_R(\Delta T_L)|}{|J_L(\Delta T_R)| + |J_R(\Delta T_L)|}. \quad (11)$$





**Figure 8.** Heat currents in response to the different temperature gradients as functions of the quantum dot gate voltages in the maximally correlated configuration, with  $\Gamma_{L1} = \Gamma_{R0} = 0$ . Note that the heat currents  $J_L, J_R$  change sign when the gradient is applied to the opposite terminal in the conductor. In that case also, they are centered at different triple points. The rest of the parameters is as in figure 3.

An ideal thermal diode operates at  $\mathcal{R} \approx 1$ . We emphasize that, due to the presence of the gate terminal, heat is not conserved in the conductor subsystem and therefore  $\mathcal{R}$  requires two currents to be defined. A symmetric configuration as the one considered in figure 3 obviously gives  $\mathcal{R} = 0$ .

Finite rectification coefficients are obtained for a simple left–right asymmetric configuration,  $\Gamma_{ln} = \Gamma_l$ . This case can be understood by considering for example the case  $\Gamma_L \gg \Gamma_R$ . An electron residing in the left terminal will easily get into the dot, but once there, it takes a longer time to tunnel through the right barrier. During this time, it is in contact with the gate reservoir. On the other hand, left moving electrons hardly enter the dot, but then they can rapidly tunnel to the left. Therefore, the time that left- and right-moving electrons spend in contact with the gate reservoir is different, and so is the probability that they lose heat in it. As a consequence, the heat current arriving to the left terminal when heating the right one will be larger. The role of the gate is totally passive in this case, only acting as a heat sink.

A configuration that emphasizes the left–right asymmetric energy-dependent rates suppresses tunneling processes through different barriers at different energies, for instance:  $\Gamma_{L0} = \Gamma_{R1} = \Gamma$ , and  $\Gamma_{L1} = \Gamma_{R0} = x\Gamma$ . Let us first consider for simplicity the case  $x = 0$ . Then transitions  $(0, n) \leftrightarrow (1, n)$  only occur through the left barrier for  $n = 0$  and through the right one, for  $n = 1$ . In section 6 we propose an implementation of this configuration. It also corresponds to an optimal (Carnot efficient) heat engine [11], and provides a maximal correlation between the different flows [70]:

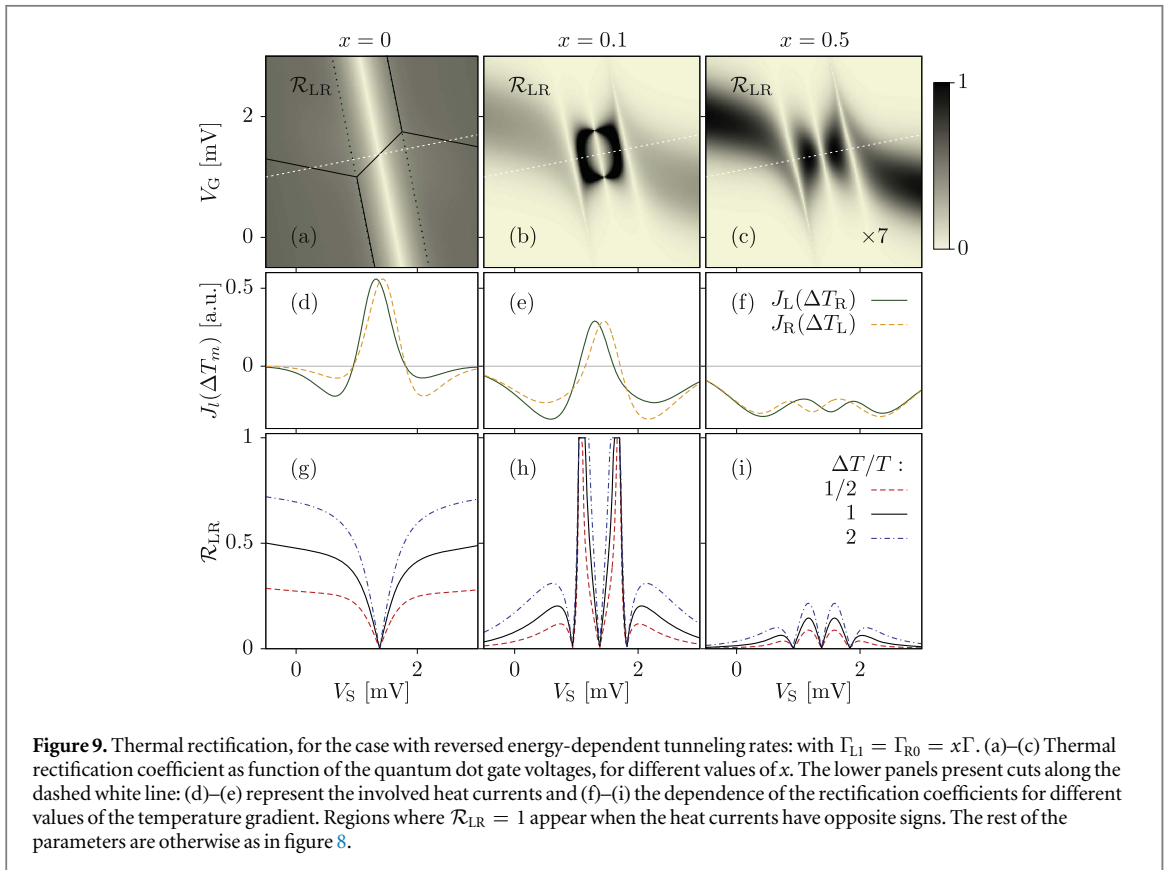
$$\frac{J_L}{\Delta U_{S0}} = -\frac{J_R}{\Delta U_{S1}} = \frac{J_G}{E_C} = \mathcal{I}, \quad (12)$$

where

$$\mathcal{I} = \frac{\Gamma_{L0}^+ \Gamma_{R1}^+ \Gamma_{G0}^+ \Gamma_{G1}^+}{\gamma^3} \frac{\Delta U_{G0}}{e^{k_B T_G}} \left( e^{\frac{\Delta U_{S1}}{k_B T_R}} - e^{\frac{\Delta U_{S0}}{k_B T_L}} e^{\frac{E_C}{k_B T_G}} \right) \quad (13)$$

is the particle current. The denominator  $\gamma^3$  is determined by the normalization of the occupation probabilities. Note that if only one terminal is hot,  $\mathcal{I} \neq 0$  for finite  $E_C$ . An electron can only be transported across the conductor if it exchanges an energy  $E_C$  with the gate. This property, which is usually known as tight energy-matter coupling, here applies to all heat fluxes in the system.

In figure 8, the different heat currents are displayed for the temperature gradient applied to the different terminals. They occur only around the stability vertex where energy can be exchanged with the gate. Each current is closer to a different triple point, corresponding to the charge configuration at which tunneling is



permitted. In agreement with equations (12) and (13), when the temperature gradient is applied to one of the conductor terminals,  $l$ , the corresponding heat current  $J_l$  vanishes (but does not change sign) when  $\Delta U_{s0} = 0$  ( $l = L$ ) or when  $\Delta U_{s1} = 0$  ( $l = R$ ).

### 5.1. Cooling by (really) heating

Very remarkably, the current at the opposite terminal vanishes at two points, when  $\Delta U_{sn} = 0$ , where it changes sign. As a consequence, we find configurations in the center of the stability vertex where heat is extracted from the two terminals of the conductor,  $J_L, J_R > 0$ , i.e. by heating one of them, the other one gets cooled. The excess heat is absorbed by the gate system. Hence only in the strictly hot terminal, our setup satisfies the Clausius statement that heat flows from hot to cold in the absence of work done onto the system. We also find heat flowing between two cold reservoirs. Differently from other proposals of cooling by heating [87–89], here we do not couple to an incoherent source that drives a particular transition, but rather really heat one part of the system up.

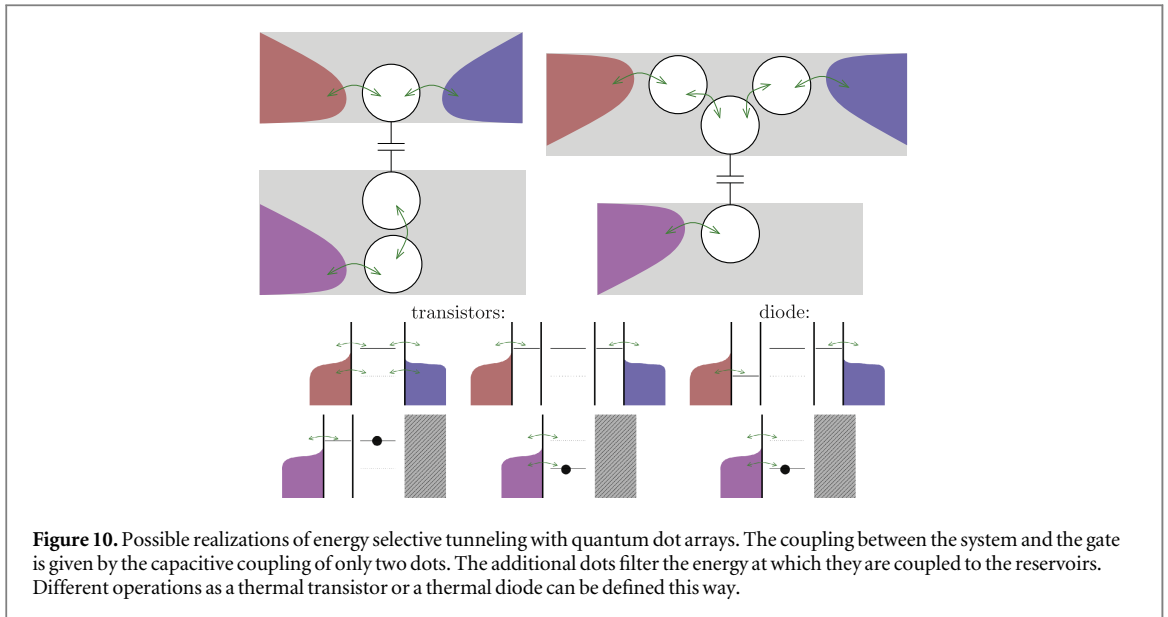
Similar effects have been found for two finite systems coupled by energy filters [90]. In our case, this is a dynamical effect due to the coupling to the gate, which enables the transported electrons to tunnel at different energies depending on the involved lead. Related properties have been described for asymmetric quantum dots in the dynamical Coulomb blockade regime [43], suggesting the possibility to define thermal devices by properly engineering the coupling to their environment.

### 5.2. Thermal rectification

Let us concentrate on the thermal rectification. In figure 8, one can clearly observe an asymmetry of the heat currents due to an opposite gradient:  $J_l(\Delta T_j) \neq J_l(\Delta T_i)$ . It is due to the heat currents being largest at different dot potentials for different terminals. The thermal rectification coefficient will therefore be finite, except for the case when the system is equidistant from the conditions  $\Delta U_{s0} = 0$  and  $\Delta U_{s1} = 0$ , as shown in figure 9 for  $x = 0$ . It increases with the detuning of the conductor level with respect to the Fermi energy, where on the other hand the currents are exponentially suppressed. Interestingly,  $\mathcal{R}$  increases with the applied temperature gradient,  $\Delta T$ , and gets closer to  $\mathcal{R} = 1$  for larger gradients.

### 5.3. Leakage currents: thermal diode

Remarkable deviations from this behavior appear for  $x \neq 0$ . In this case, a small current will leak at *undesired* energies at each of the terminals. This modifies the conditions at which the heat currents vanish. In particular,



$J_L(\Delta T_R)$  and  $J_R(\Delta T_L)$  change sign at different points, see figure 9 for  $x = 0.1$ . As a consequence, two small voltage windows open when they are opposite in sign, i.e. they have the same direction. Within these windows, the system behaves as an ideal thermal diode, with  $\mathcal{R} = 1$ . The size of the windows increases with the applied temperature gradient.

For larger leakage currents, the cooling by heating effect disappears, so both  $J_L(\Delta T_R)$  and  $J_R(\Delta T_L)$  are negative, see figure 9 for  $x = 0.5$ . They are still different, in general, and hence a finite but small rectification coefficient is obtained.

## 6. Quantum dot arrays for energy filtering

We end by analyzing the experimental feasibility of the different configurations discussed above. The energy-dependent rates of systems of two coupled quantum dots can be modified by means of gate voltages [12]. However, even if configurations with large enough asymmetries can be found [64], they are very difficult to control.

One can however think of more complicated quantum dot arrays. The discrete level of the outermost quantum dots can be used as energy filters which can be tuned externally. The coupling between the conductor and gate subsystems is mediated by only two dots, as sketched in figure 10. This way, tunneling from the different terminals can be put in resonance with the required configurations at  $\Delta U_{im}$ , as long as the width of the filter levels is smaller than  $E_C$  [91].

The simplest case, as it only involves one additional barrier, is when the gate contains a double quantum dot. The one connected to the reservoir behaves as a zero-dimensional contact [92]. Its level can be chosen to inject electrons only either at  $\Delta U_{G0}$  or  $\Delta U_{G1}$ , thus providing a configuration with either  $\Gamma_{G1} = 0$ , or with  $\Gamma_{G0} = 0$ , respectively. They would work as thermal transistors around different triple points in the stability diagram [82].

Controlling tunneling in the conductor (as discussed in this work) would require a triple quantum dot, see figure 10. Fine tuning of such structures has been achieved in the last decade [93–96]. On the other hand, it permits for a more flexible operation of the system: if the two filters are resonant with the same state,  $\Delta U_{im}$ , the rates with  $n' \neq n$  will vanish ( $\Gamma_{n'} = 0$ ), and the system is a thermal transistor, as discussed in section 4. If now one of the filters is put in resonance with the other state, it works as a thermal diode or a refrigerator, see section 5. We can therefore change the operation of the device from a transistor to a diode by just changing a gate voltage.

## 7. Conclusions

We have investigated the properties of electronic heat transport in a system of capacitively coupled quantum dots in a three-terminal configuration. One of the dots acts as a mesoscopic thermal gate which can either serve as a heat source or sink, or control the occupation of the other dot. Heat exchange mediated by electron–electron interactions introduces different ways to tune the energy-dependence of the relevant tunneling events.

All-thermal control of heat currents can be achieved by controlling the appropriate system asymmetries. It allows us to define different operations such as a thermal transistor, a thermal diode, and a refrigerator based on the interaction with the gate system. On one hand, dynamical channel blockade of the conductor heat currents via charge fluctuations in the gate enable a thermal transistor with huge amplification factors. On the other hand, the correlation of state-dependent transitions in the three different contacts rectifies the heat currents and induces the cooling of one terminal by the heating of the other one. These two effects combine in the operation of an ideal thermal diode with  $\mathcal{R} = 1$ .

The different configurations can be implemented nowadays, under experimental state of the art. In arrays of quantum dots, the optimum level of performance can be achieved. Our results consider realistic parameter estimations from the experiment [12].

Our work uses a mesoscopic structure to mediate the coupling of the conductor with the thermal environment. Working as a switch or inducing inelastic transitions, the mediator defines the different behaviors of the system. This strategy opens the possibility to use engineered system-environment couplings to improve or define new functionalities.

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