

# Uncovering dispersion properties in semiconductor waveguides to study photon-pair generation

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## Abstract

We investigate the dispersion properties of ridge Bragg-reflection waveguides to deduce their phasematching characteristics. These are crucial for exploiting them as sources of parametric down-conversion (PDC). In order to estimate the phasematching bandwidth we first determine the group refractive indices of the interacting modes via Fabry–Perot experiments in two distant wavelength regions. Second, by measuring the spectra of the emitted PDC photons, we gain access to their group index dispersion. Our results offer a simple approach for determining the PDC process parameters in the spectral domain, and provide important feedback for designing such sources, especially in the broadband case.

Keywords: Bragg-reflection waveguide, parametric down-conversion, phasematching, group refractive index

(Some figures may appear in colour only in the online journal)

## 1. Introduction

Non-linear optics provides a variety of different frequency conversion processes for implementing diverse photonic states for quantum informatics. Particularly intriguing is the process of parametric down-conversion (PDC) known for producing photon-number correlated twin beams at a few photon level. Due to their rich spectral structure, only very few of these sources intrinsically emit light into a single optical mode [1, 2]. Yet, despite the spectral multimodeness, many of the conventional PDC sources are still capable of producing indistinguishable photon pairs [3]. Otherwise their output needs to undergo further state manipulation, such as

filtering, before being applicable to quantum optics tasks, causing an inevitable decrease in brightness.

The spectral properties of photon pairs created in the PDC process, which obeys energy and momentum conservation, depend both on the pump laser spectrum and on the phasematching condition in the second order non-linear optical material. Together they result in a joint spectral distribution (JSD) of the twin beams—typically called signal and idler [4, 5]. The standard way to measure the JSD is to scan over the signal and idler frequencies while detecting the coincident photons [6–11]. This is usually either time consuming or takes a lot of experimental effort. It is possible to reduce the required resources via compressed sensing, as demonstrated by observing the PDC impulse correlations [12]. Recently, seeded PDC [13, 14] has also been utilized to gain faster and better imaging of the JSD. In this case, the seed beams determine the spectral resolution. Also, sum-frequency generation provides a direct mapping of the spectral correlations [15].



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Rastering the JSD with good resolution becomes a big effort if signal and idler span several tens of nanometers [16, 17]. The characteristics of the joint spectrum are mostly governed by the phasematching between the interacting modes that stem from their group indices. Luckily, the group index can be accessed, even in highly multimodal PDC waveguides, such as Bragg-reflection waveguides (BRWs) via Fabry–Perot oscillations [18–21]. Thus, the spectral characteristics of the PDC emission can, in principle, be predicted even without non-linear interaction using *linear optical experiments* only.

BRWs based on AlGaAs have become appealing for producing spectrally broadband and indistinguishable twin photons [22, 23] and for generating entanglement [24, 25], using modal phasematching between the co-propagating signal, idler and pump modes. In other words, at least one of the interacting modes is a higher order mode [26, 27]. Even though accurate measurements of the refractive index of bulk AlGaAs exist [28], the effective indices of different spatial modes propagating in BRWs can usually be investigated only numerically [29–31]. While the refractive index can be simulated quite accurately, the group index calculated from these models can be far from the true experimental value. This makes accurate predictions of the JSD very challenging.

Recently, we used Fabry–Perot measurements in BRWs to accurately measure the group index of the pump [21]. Here, we apply this method also in the down-conversion wavelengths to obtain the phasematching bandwidth of our BRWs. The precision of the used method depends only on the spectral properties of the measured Fabry–Perot fringes. Moreover, we record the spectra of the individual twin beams at the few-photon level to further gain information about their group index dispersion. Our results provide straightforward access to the spectral PDC process parameters and are useful for optimizing the performance of such integrated optics devices.

## 2. Theoretical background: spectral characteristics of PDC emission

The PDC twin beams, signal (*s*) and idler (*i*), are created as a squeezed vacuum, which can be approximated at low gains as [4]

$$|\Psi\rangle \sim |0\rangle + \zeta \int d\omega_s \int d\omega_i f(\omega_s, \omega_i) \hat{a}_s^\dagger(\omega_s) \hat{a}_i^\dagger(\omega_i) |0\rangle, \quad (1)$$

where  $|\zeta|^2 \ll 1$  is the photon-pair creation probability dependent on the pump strength and on the effective nonlinearity of the waveguide;  $\hat{a}_s^\dagger$  ( $\hat{a}_i^\dagger$ ) accounts for the photon creation at the frequency  $\omega_s$  ( $\omega_i$ ) and

$$f(\omega_s, \omega_i) = \frac{1}{\sqrt{\mathcal{N}}} \alpha(\omega_p) \operatorname{sinc}\left(\frac{L}{2} \Delta k(\omega_s, \omega_i)\right) e^{-i\frac{L}{2} \Delta k(\omega_s, \omega_i)} \quad (2)$$

describes the joint spectral amplitude of the PDC process taking place in an ideal non-linear optical waveguide of length  $L$  and is normalized via  $\mathcal{N}$  to

$\int d\omega_s \int d\omega_i |f(\omega_s, \omega_i)|^2 = 1$ . The pump amplitude  $\alpha(\omega_p) = \exp(-(\omega_p - \omega_p^c)^2 / \sigma_p^2)$  in equation (2) is usually described in terms of the pump frequency  $\omega_p$  by a Gaussian function with  $\sigma_p$  being its bandwidth and  $\omega_p^c$  its central frequency. Due to strict energy conservation between the signal, idler and pump  $\omega_p = \omega_s + \omega_i$ . Therefore, it is useful to express the frequencies  $\omega_\mu = \omega_\mu^0 + \nu_\mu$  in terms of detunings  $\nu_\mu$  ( $\mu = s, i, p$ ) from a phasematched frequency triplet  $\omega_p^0 = \omega_s^0 + \omega_i^0$  and rewrite the pump amplitude as

$$\alpha(\omega_p = \nu_p + \omega_p^0 = \nu_s + \nu_i + \omega_p^0) = e^{-\frac{(\nu_s + \nu_i - \Delta)^2}{\sigma_p^2}}, \quad (3)$$

in which  $\Delta = \omega_p^c - \omega_p^0$  is the detuning of the pump frequency from the phasematching.

Since in waveguided structures discrete spatial modes appear, we calculate the phase mismatch  $\Delta k(\omega_s, \omega_i)$  in equation (2) for co-propagating signal, idler and pump with the help of the effective refractive indices  $n_\mu$  describing the mode propagation and use  $k_\mu(\omega) = n_\mu(\omega) \frac{\omega}{c}$ , where  $c$  is the speed of light. In the vicinity of the phasematched point, where  $\Delta k^0 = k_s(\omega_s^0) + k_i(\omega_i^0) - k_p(\omega_p^0) = 0$ , we perform a second order series expansion of the phase mismatch by [32]

$$\begin{aligned} \Delta k(\omega_s, \omega_i) &= k_s(\omega_s) + k_i(\omega_i) - k_p(\omega_p) \\ &\approx \Delta k^0 + k'_s(\omega_s^0) \nu_s + k'_i(\omega_i^0) \nu_i - k'_p(\omega_p^0) \nu_p \\ &\quad + k''_s(\omega_s^0) \frac{\nu_s^2}{2} + k''_i(\omega_i^0) \frac{\nu_i^2}{2} - k''_p(\omega_p^0) \frac{\nu_p^2}{2}, \end{aligned} \quad (4)$$

in which  $k'_\mu(\omega) = n_\mu^g(\omega)/c$  is related to the group index of the mode given by  $n_\mu^g(\omega) = n_\mu(\omega) + \omega \frac{dn_\mu(\omega)}{d\omega}$  and  $k''_\mu(\omega) = \frac{1}{c} \frac{dn_\mu^g(\omega)}{d\omega}$  is determined by its dispersion. The more compact expression

$$\begin{aligned} \Delta k &= \kappa_s \nu_s + \kappa_i \nu_i \\ &\quad + \frac{1}{2} (K_s - K_p) \nu_s^2 + \frac{1}{2} (K_i - K_p) \nu_i^2 - K_p \nu_s \nu_i \end{aligned} \quad (5)$$

with  $\kappa_s = k'_s(\omega_s^0) - k'_p(\omega_p^0)$ ,  $\kappa_i = k'_i(\omega_i^0) - k'_p(\omega_p^0)$ ,  $K_s = k''_s(\omega_s^0)$ ,  $K_i = k''_i(\omega_i^0)$  and  $K_p = k''_p(\omega_p^0)$  is useful for extracting the slope of the phasematching in signal and idler frequency space by following a constant phasematching contour via

$$\frac{\partial \Delta k}{\partial \nu_i} \Delta \nu_i + \frac{\partial \Delta k}{\partial \nu_s} \Delta \nu_s = 0. \quad (6)$$

This results in the slope or so-called phasematching tilt of

$$\frac{\Delta \nu_i}{\Delta \nu_s} = -\frac{\kappa_s + K_s \nu_s - K_p \nu_p}{\kappa_i + K_i \nu_i - K_p \nu_p}, \quad (7)$$

which represents the ratio of the group index differences from the twin beams to the pump and is given in a more general form by

$$-\frac{[n_s^g(\omega_s^0 + \nu_s) - n_p^g(\omega_p^0 + \nu_p)]}{[n_i^g(\omega_i^0 + \nu_i) - n_p^g(\omega_p^0 + \nu_p)]}.$$

## 2.1. Phasematching in the linear dispersion regime

In order to estimate the spectral characteristics of the PDC emission, it is often adequate to consider only the first order terms in equation (5). This is typically done in the vicinity of  $\Delta \approx 0$ . Further, as we are only interested in the full width at half maximum (FWHM) of the phasematching, we replace the sinc-function in equation (2) with a Gaussian approximation by adapting their bandwidths via a constant factor  $\gamma$  [32, 33]. Thus, we estimate that  $\text{sinc}[\Delta k(\omega_s, \omega_i)L/2] \approx e^{-\gamma[\Delta k(\omega_s, \omega_i)L/2]^2}$ . Putting equations (3) and (5) into equation (2) we re-express it as 2D-Gaussian in the form [33]

$$|f(\omega_s = \omega_s^0 + \nu_s, \omega_i = \omega_i^0 + \nu_i)| \propto \exp \left( -[\nu_s \ \nu_i] \begin{bmatrix} \frac{1}{\sigma_p^2} + \gamma \frac{L^2}{4} \kappa_s^2 & \frac{1}{\sigma_p^2} + \gamma \frac{L^2}{4} \kappa_s \kappa_i \\ \frac{1}{\sigma_p^2} + \gamma \frac{L^2}{4} \kappa_s \kappa_i & \frac{1}{\sigma_p^2} + \gamma \frac{L^2}{4} \kappa_i^2 \end{bmatrix} \begin{bmatrix} \nu_s \\ \nu_i \end{bmatrix} \right) \quad (8)$$

The eigenvalues of the correlation ellipse in equation (8) are given by [34]

$$\frac{1}{\sigma_{\pm}^2} = \frac{1}{\sigma_p^2} + \frac{\gamma L^2}{8} (\kappa_s^2 + \kappa_i^2) \pm \sqrt{\frac{1}{\sigma_p^4} + \left( \frac{\gamma L^2}{8} (\kappa_s^2 + \kappa_i^2) \right)^2 + \frac{1}{\sigma_p^2} \frac{\gamma L^2}{2} \kappa_s \kappa_i} \quad (9)$$

corresponding to the minor and major semiaxes of the correlation ellipse. They can be estimated if the group indices of the signal, idler and pump, as well as the pump bandwidth and the waveguide length, are known. We are only interested in the phasematching bandwidth  $\sigma_{\text{PM}}$  that corresponds to the minor semiaxis in equation (9) after letting  $\sigma_p \rightarrow \infty$  and obtain [34]

$$\frac{1}{\sigma_{\text{PM}}^2} = \gamma (\kappa_s^2 + \kappa_i^2) \frac{L^2}{4}. \quad (10)$$

## 2.2. Phasematching in the curved dispersion profile

In general, however, the group index dispersion is non-negligible causing bending of the phasematching curve so that equation (7) does not remain constant. We investigate the case in which the phasematching contour is probed by measuring the spectral extent of the signal and idler single counts, in other words their *marginal spectra*, with a continuous wave (CW) pump. For the signal beam this spectrum can be calculated from equation (1) by letting the pump spectrum  $|\alpha(\omega_p)|^2 \rightarrow \delta(\omega_p - \omega_p^c)$ , while tracing over the idler frequency and projecting the signal on a varying frequency. If the measurement can be done with a high resolution spectrograph, the signal marginal spectrum yields

$$|f(\omega_s = \omega_s^0 + \nu_s)|^2 \propto \left| \text{sinc} \left( \frac{L}{2} \Delta k(\omega_s, \omega_i = \omega_p^c - \omega_s) \right) \right|^2. \quad (11)$$

In a similar manner, the idler marginal spectrum can be extracted. Thus, by recording the marginal spectra, we

investigate the phase mismatch  $\Delta k$  in equation (5) under the condition  $\nu_s + \nu_i = \Delta$  and rewrite

$$\Delta k = \kappa_s \nu_s + \kappa_i \nu_i + \frac{1}{2} K_s \nu_s^2 + \frac{1}{2} K_i \nu_i^2 - \frac{1}{2} K_p \Delta^2 = 0, \quad (12)$$

from which the central frequencies of the signal and idler can be solved. Typically, the pump detuning is much smaller than the shift in the signal and idler frequencies ( $\Delta \ll \nu_{s,i}$ ). Therefore, at low pump detunings the bending of the phasematching curve is rather insensitive to the group index dispersion of the pump beam and is dominated by that of signal and idler.

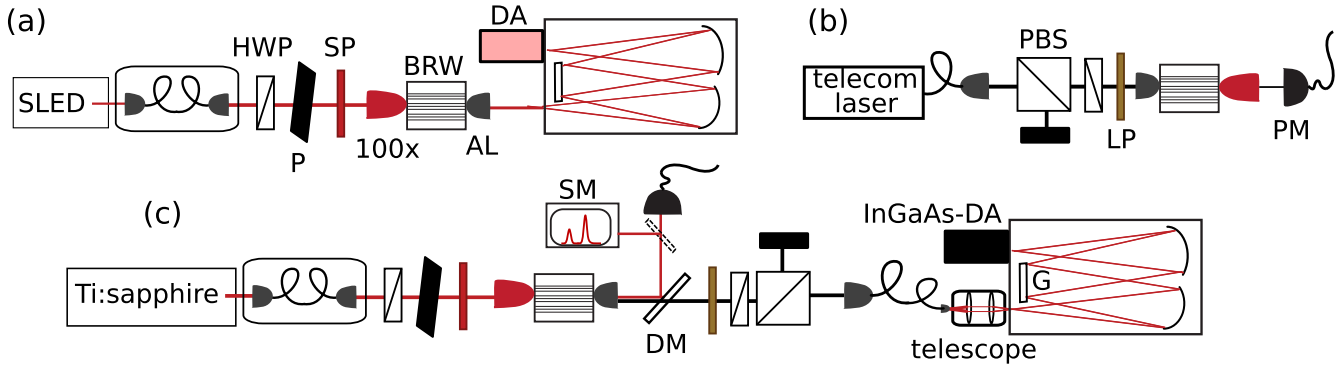
## 3. Experiment

In our experiments, we use two different BRW samples, both fabricated from the same grown wafer as in [21, 23]. Ridge waveguides were defined via electron beam lithography followed by reactive ion plasma etching. The sample used in the Fabry–Perot measurements is 996(4)  $\mu\text{m}$  long and has a ridge width of 6  $\mu\text{m}$ . It is uncoated and etched down to the layer beneath the core. Meanwhile, the sample employed in the measurement of the marginal spectra is about 1.87 mm long and has a ridge width of 4  $\mu\text{m}$ . It has an anti-reflection coating on the front facet for the pump wavelengths and is etched to the layer above the core.

Both samples are phasematched for a type-II PDC process between the near infrared (NIR) pump in a higher order Bragg mode and signal and idler in the telecommunication band close to 1550 nm. Signal and idler are cross-polarized total-internal reflection (TIR) modes—the BRW's fundamental spatial modes. According to our experience, the utilization of BRWs with different ridge widths and etch depths only slightly alters the dispersion characteristics, causing a shift in the phasematching wavelength that can be about 10 nm, nevertheless, small in relative scale. Therefore, the results gained from waveguides with the same layer structure are comparable.

Our experimental setups are shown in figure 1. For the Fabry–Perot measurements in the NIR we employ in figure 1(a) a broadband super-luminescent light emitting diode (SLED) with a central wavelength of 777 nm and an FWHM of about 17 nm as a light source. Its beam is mode cleaned and sent through a half-wave plate (HWP) and a sheet polarizer (P) for power and polarization control. A short pass (SP) spectral filter guarantees that the beam is clean from undesired wavelength contributions. A 100 $\times$  microscope objective couples the light to the BRW under study and an aspheric lens with a focal length of 3.1 mm collects the light afterwards. After that, the NIR light is directed to a spectrograph with 10 pm resolution and recorded with a detector array (DA) sensitive in the range from 400–1000 nm for observing the Fabry–Perot fringes, as in [21].

For the transmission measurements in the telecommunication range we couple in figure 1(b) a tunable CW laser via a polarizing beam splitter (PBS) and a HWP that



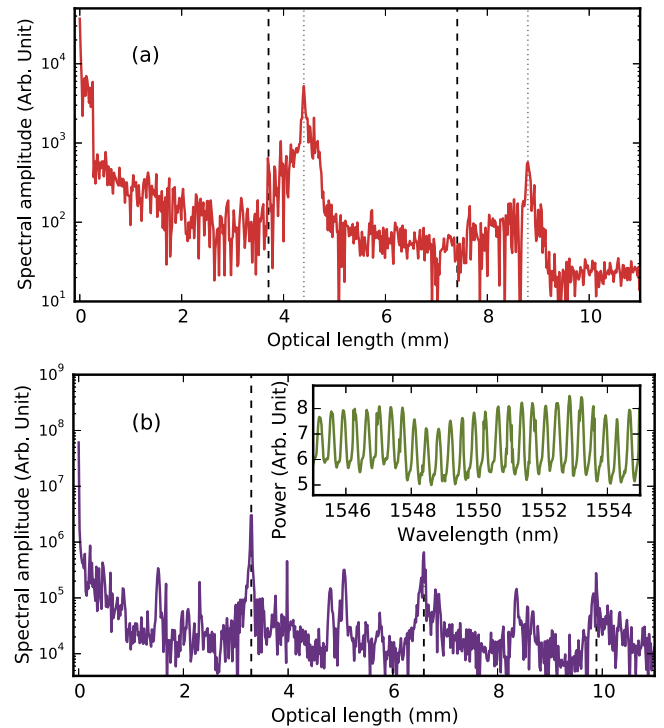
**Figure 1.** Experimental setups for measuring both the Fabry–Perot fringes in the (a) NIR and (b) telecommunication ranges and (c) the marginal spectra of the PDC emission. For more information and abbreviations see text.

controls the polarization in the backward direction to our BRW. The Fabry–Perot fringes are measured in the spectral range from 1523–1594 nm with a power meter (PM).

For measuring the marginal spectra in figure 1(c) we slightly modify the setup in figure 1(a). We now employ a CW Ti:sapphire laser as a pump. After passing through the BRW, the pump is separated from the light in the telecommunication range with a dichroic mirror (DM) and sent either to a spectrometer (SM) having a resolution of about 0.3 nm or to the PM. The pump power coupled through the BRW is kept constant at approximately 0.6 mW. The PDC emission then passes a long-pass (LP) filter, which suppresses background light below 1.4  $\mu\text{m}$ , and gets coupled in a polarization-selective manner to a grating spectrometer mounted to an InGaAs-detector array (InGaAs-DA) operating at  $-40^\circ\text{C}$ . A single exposure can record a spectral band of about 110 nm. In order to cover a larger bandwidth, its grating (G) is moved with a motorized stage. The acquisitions are stitched together via calibration points recorded with a tunable narrowband CW telecom laser, resulting in a total resolution of about 1 nm per pixel. Moreover, our InGaAs-DA has a sharp cut-off for wavelengths longer than approximately 1.65  $\mu\text{m}$ .

#### 4. Accessing phasematching bandwidth via group index

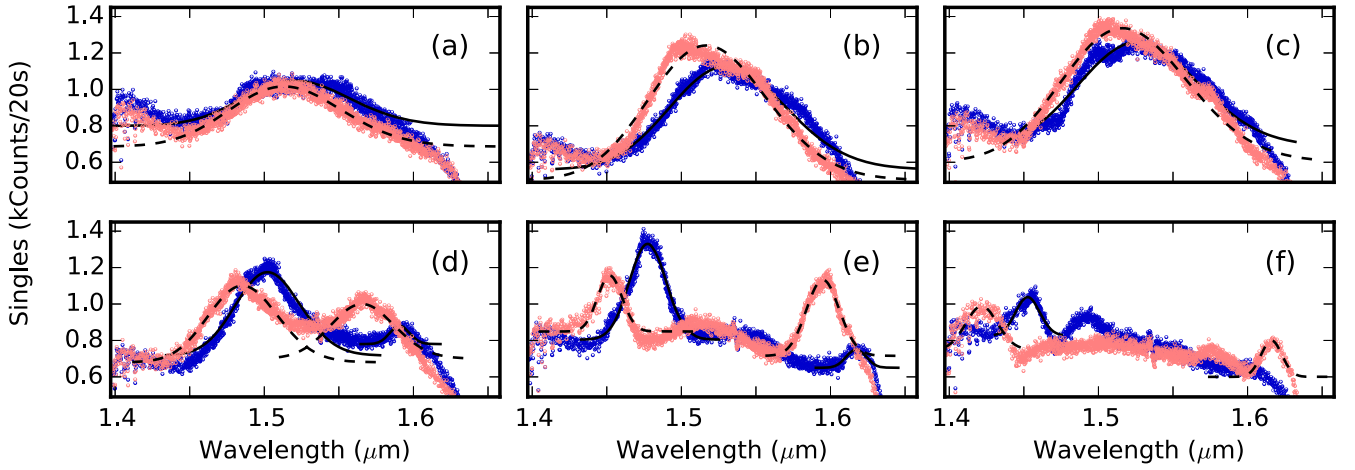
We start by measuring the Fabry–Perot fringes in order to find out the group indices of the Bragg and TIR modes and to extract the phasematching bandwidth. In figures 2(a)–(b) we show the Fourier transforms of the recorded fringes, while the inset in figure 2(b) shows the raw data in a small wavelength range near 1550 nm. Repeating peaks in the Fourier domain appear at multiples of the optical length given by  $n_m^g L$  in terms of the group index of the excited mode ( $m$ ). As expected, we see that the waveguide is highly multimodal in the NIR. The TIR mode is most prominent and only a portion of the light is coupled to the Bragg mode, which is identified in a way similar to that in [21] as the mode with the lowest apparent group index. In the telecommunication range, practically only the TIR mode is excited and the peaks



**Figure 2.** Fourier transformation of the measured Fabry–Perot oscillations in the (a) NIR and (b) telecommunication ranges. The inset in (b) shows a snapshot of the recorded fringes. Due to high losses in the NIR, the second repeating peak is only evident for the TIR mode and that of the Bragg mode disappears in the noise floor. The dashed lines show the position of the desired modes, whereas the dotted lines indicate the TIR mode in the NIR having the group index of 4.42(3).

appearing in between the repeating peaks are most probably caused by other experimental imperfections, such as fluctuations of the CW laser.

Taking into account the waveguide length, we obtain 3.31(2) and 3.72(3) for the group indices of the TIR and Bragg modes at the PDC and pump wavelengths, respectively. In order to infer the phasematching bandwidth in the short BRW, we plug the measured optical lengths directly to equation (10), which causes the resonator length to cancel out. Thus, the accuracy is solely given by the number of measured Fabry–Perot fringes and by their spectral resolution.



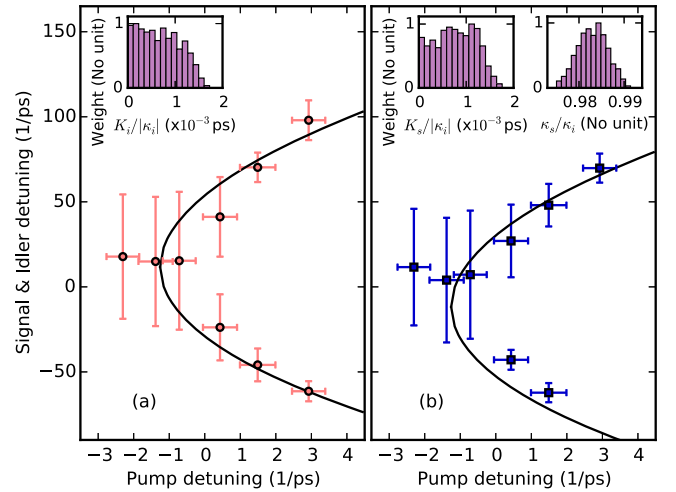
**Figure 3.** Marginal spectra of signal and idler measured at the pump wavelengths (a) 768.3 nm (b) 768.0 nm (c) 767.8 nm, (d) 767.5 nm, (e) 767.1 nm and (f) 766.7 nm. Light red (dark blue) symbols indicate the measured values for idler (signal), whereas the solid and dashed lines show Gaussian fits for the found peaks. The second small peaks in (f) may be caused by laser instabilities or another phasematched process nearby.

Regarding the joint spectral intensity,  $\gamma = 0.179$  [35] that adapts the FWHM of the squared sinc-function to that of squared Gaussian and we receive for the phasematching bandwidth a FWHM of 3.7(3) nm. Finally, the group index difference between the PDC and pump modes divided by the speed of light is  $(-1.37 \pm 0.12) \text{ ps } \mu\text{m}^{-1}$  that we call  $\bar{\kappa}$ . We note that this is an averaged value over the measured spectral ranges. Unfortunately, the fringe measurement is not accurate enough to resolve the differences between signal and idler. Therefore, we study their marginal spectra at a few photon level next.

## 5. Accessing group index dispersion via marginal spectra

In order to gain information regarding the group index dispersion, we record the marginal spectra of the signal and idler at different pump wavelengths. Thus, we tune the pump near the degeneracy, which was observed by measuring the second-harmonic light from our BRW at the fundamental wavelength of 1535.2 nm. Figure 3 illustrates the recorded spectra. We clearly notice that they gradually split up into two spectral bands, i.e. have two maxima both for the signal and idler. This hints at a non-negligible group index dispersion at PDC wavelengths such that equation (12) has two solutions. Further, we note that there is a shift between the central wavelengths of the signal and idler, implicating a small difference in their group indices, which we could not resolve with our measurements in section 4.

In figure 4, we show the fitted central frequencies for the signal and idler as detunings from the degeneracy with respect to that of the pump. We see a slight offset in signal and idler detunings close to the degeneracy, which we believe is an artefact caused by limitations in the spectral sensitivity of our InGaAs-DA. We further note that the signal and idler marginal spectra are about 90 nm wide near degeneracy making the accurate search of central frequencies from rather flat



**Figure 4.** The measured frequency detunings (symbols) with respect to that of the pump for (a) idler (b) signal. The vertical errorbars mark the FWHM of the measured spectra, whereas the horizontal ones indicate the spectral resolution of the bright light spectrometer. Solid lines represent the phasematching curve simulated with the parameters found with the Monte Carlo optimization. The insets show histograms for  $\kappa_s$  and  $K_{s,i}$  received from the Monte Carlo simulation.

distributions challenging. Additionally, there is a small discrepancy between the pump detuning ( $\Delta$ ) and that of the signal ( $\nu_s$ ) and idler ( $\nu_i$ ), for which we ideally expect  $\Delta = \nu_s + \nu_i$ . We track this to a calibration shift between the detectors. While the InGaAs-DA is calibrated with the tunable CW laser, the pump wavelengths are measured with a separate bright light spectrometer. We match these two devices by measuring the wavelength of the second-harmonic light. However, a small offset in pump detuning still remains.

We employ Monte Carlo simulations to find the PDC process parameters for our BRW in the spectral domain. For this purpose, we must plug in some *a priori* information into equation (12) since it has multiple solutions. First, we

simulate all parameters with respect to  $\kappa_i$ , as all found solutions multiplied by a constant factor still fulfil equation (12). We then utilize the information gained from section 4 in order to receive the correct phasematching width. Second, we limit the group index of the signal beam to values higher than that of the idler, as expected from the measured spectra. Third, we expect that the signal and idler properties only differ slightly from each other and that their group indices only have low dispersion over the measured spectral region. The latter can be justified from the broadband Fabry–Perot experiment [21]. Finally, we investigate the phasematching properties with rather small pump detunings. In other words, while the splitting of the upper and lower spectral bands in figure 3 is maximally on the order of 200 nm, that of the pump is less than 2 nm. Therefore, we disregard the term  $1/2K_p\Delta^2$  in equation (12).

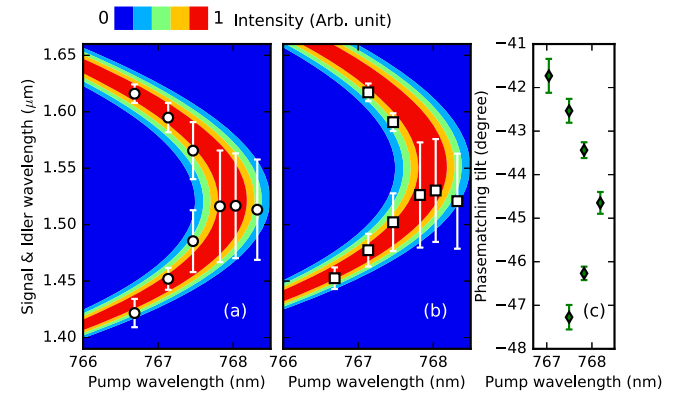
A Monte Carlo simulation with  $10^6$  runs optimizes the parameters  $\kappa_s$ ,  $K_s$ ,  $K_i$ , while a small offset in the detuning  $\Delta$  is allowed. The simulation generates these parameters from uniform distributions of large parameter ranges and accepts only those sets, for which the contour  $\Delta k = 0$  lies within the vertical errorbars shown in figure 4. We exclude the lower sideband of the signal beam in figure 4(b) from the fit due to the sharp cut-off in the sensitivity of our InGaAs-DA at higher wavelengths. However, we emphasize that even if only one marginal spectrum was measured, the other one can be accurately predicted by the fitted parameters. The histograms gained for  $\kappa_s$ ,  $K_s$  and  $K_i$  are shown in the insets in figure 4. Due to the fact that all signal detunings reside at lower frequencies than those of the idler, a small group index difference of signal and idler emerges as expected. Additionally, sharp upper limits appear for  $K_s$  and  $K_i$  that are determined by the respective group index dispersions. These parameters decide how strongly the upper and lower frequency bands in figure 4 bend together with respect to the pump detuning. They also tend to opposite directions such that a large value in the signal beam is compensated by a lower one in the idler one, or vice versa.

## 6. Phasematching in BRWs

To summarize, we present in table 1 the dispersion properties found in sections 4 and 5 that govern the spectral properties of the PDC emission. By combining our results from the two experiments, we can predict the characteristics of the PDC emission. Figures 5(a)–(b) show good agreement between this prediction and the results for the marginal spectra. We can further approximate that the group index difference between the signal and idler at 1550 nm is about  $(7.0 \pm 1.5) \cdot 10^{-3}$ . This causes a slight temporal delay between the signal and idler wavepackets when leaving BRW. Moreover, figure 5(c) illustrates the phasematching tilt as a function of the pump wavelength for the measured central frequencies of the signal and idler. It indicates slight bending of the phasematching contours in frequency space caused by the group index dispersion.

**Table 1.** Parameters governing the spectral properties of PDC emission retrieved from the Fabry–Perot (FB) experiment in section 4 and via Monte Carlo (MC) optimization for the marginal spectra in section 5.

	Dispersion parameter	Value
FP	$n_{\text{TIR}}^g$ at 775 nm	4.42(3)
	$n_{\text{Bragg}}^g$ at 775 nm	3.72(3)
	$n_{\text{TIR}}^g$ at 1550 nm	3.31(2)
	$\bar{\kappa}$ ( $\times 10^{-3}$ ps/ $\mu\text{m}$ )	$-1.37 \pm 0.12$
	PM bandwidth (nm)	$3.7 \pm 0.3$
MC	$\kappa_s/\kappa_i$	0.983(4)
	$K_s/ \kappa_i $ ( $\times 10^{-3}$ ps)	0.8(5)
	$K_i/ \kappa_i $ ( $\times 10^{-3}$ ps)	0.7(5)



**Figure 5.** Predicted (contours) and measured (symbols) spectral properties for (a) idler and (b) signal in terms of the pump wavelength together with (c) the phasematching tilt calculated by taking the arctangent from the slope in equation (7). The errorbars in (c) include only statistical variations from the Monte Carlo simulation.

## 7. Conclusions

The dispersion profile of a non-linear optical material determines its phasematching characteristics and thus mainly dictates the spectral characteristics of the PDC emission. Apart from the exact phasematching wavelength given by the effective index matching of the interacting pump, signal and idler modes, the knowledge of the group refractive index and its dispersion are crucial for predicting the properties of the signal and idler. We have utilized the well-known Fabry–Perot method to access the group indices at the pump and PDC wavelengths in order to estimate the phasematching bandwidth. Additionally, we have recorded spectral marginal distributions for the signal and idler to infer their group index difference and to acquire an approximation for their group index dispersion. Our results demonstrate a straightforward method to access the spectral PDC process parameters by making only few frequency-resolved measurements and provide the means for verifying and controlling the performance of highly sophisticated, multi-layered PDC emitters.

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