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Evolution of density and patch-size dependent dispersal rates

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Summary

Based on a marginal value approach, we derive a non-linear expression for evolutionarily stable (ES) dispersal rates in a metapopulation with global dispersal. For the general case of density-dependent population growth, our analysis shows that individual dispersal rates should decrease with patch capacity and – beyond a certain threshold – increase with population density. We performed a number of spatially explicit, individual-based simulation experiments to test these predictions and to further explore the relevance of variation in the rate of population increase, density-dependence, environmental fluctuations and dispersal mortality on the evolution of dispersal rates. They confirm the predictions of our analytical approach. In addition, they show that dispersal rates in metapopulations mostly depend on dispersal mortality and inter-patch variation in population density. The latter is dominantly driven by environmental fluctuations and the rate of population increase. These conclusions are not altered by the introduction of neighbourhood-dispersal. With patch capacities in the order of 100 individuals, kin-competition seems to be of negligible importance for ES dispersal rates except when overall dispersal rates are low.

1. Introduction

With the growing awareness of the importance of spatial aspects in ecology (Tilman & Kareiva 1997, Bascompte & Solé 1998), dispersal is increasingly considered to be an ecological key-process. For example, dispersal plays a significant role for the coexistence of species (Comins & Noble 1985, Rohani et al. 1996, Dieckmann et al. 1999, Hastings & Gavrilets 1999, Hovestadt et al. 2000). Depending on landscape structure and population parameters, dispersal also has a multitude of effects on the spatial and temporal structure of populations (Hastings 1993, Doebeli 1995, Olivieri et al. 1995, Ruxton 1996, Travis & Dytham 1998, Gyllenberg et al. 1999, Lande et al. 1999, Jang & Mitra 2000, Kean & Barlow 2000, Kendall et al. 2000). In addition, the interest in dispersal has been actuated by the needs of conservation biologists to develop strategies suited for the management of fragmented populations (den Boer 1990, Poethke et al. 1996a, Appelt & Poethke 1997, Hanski 1999, Roland et al. 2000, Thomas 2000).

To understand the evolution of dispersal strategies, we have to investigate its consequences for the (inclusive) fitness of individuals. Theoretical models have pointed out the potential role of kin competition (Hamilton & May 1977, Comins et al. 1980, Gandon & Michalakis 1999, Ronce et al. 2000a), environmental fluctuations and habitat dynamics (Venable & Brown 1993, Travis & Dytham 1999), local extinction probability (van Valen 1971, Olivieri et al. 1995, Ronce et al. 2000b), patch age (Ronce & Olivieri 1997), and patch capacity (McPeek & Holt 1992) for the evolution of conditional dispersal strategies. Recently, specific attention has been directed towards the evolution dispersal strategies sensitive to population density (Ruxton 1996, Jánosi & Scheuring 1997, Sæther et al. 1999, Travis et al. 1999, Metz & Gyllenberg 2001).

The broad spectrum of model approaches and underlying assumptions often make it difficult to judge the relevance of theoretical predictions for a particular species or landscape configuration. In this paper we will focus on the evolution of dispersal rates under conditions likely to apply to insects (e.g. grasshoppers or butterflies). Many insect species survive in patchy habitats that are object to large environmental fluctuations of patch quality (Hanski 1998); under these conditions dispersal is crucial for long-term survival of populations. The intrinsic population dynamics of insects is well studied and easy to model (Johst & Brandl 1997). In insects migration is likely to be very risky (den Boer 1990, Ward et al. 1998, Thomas & Kunin 1999, Thomas 2000), but nevertheless frequently observed (Zera

& Denno 1997); i.e. there must be large benefits associated with dispersal as well. Several studies have already demonstrated that the propensity to disperse is sensitive to population density (Herzig 1995, Baguette et al. 1996, Rhainds et al. 1997, Loxdale & Lushai 1999) and patch size (Kareiva 1985, Turchin 1986, Hill et al. 1996, Kindvall 1999, McIntyre & Wiens 1999, Kindvall & Petersson 2000, Baguette et al. 2000, Roland et al. 2000).

Travis et al. (1999) focus their individual based simulation experiments on species with non-overlapping generations, a discrete dispersal phase and a type of density dependent population growth that has been successfully used to describe the dynamics of a large number of insect populations (Bellows 1981). Thus, their approach seems to be well suited to study the evolution of dispersal in insect populations. They have shown that ES-dispersal strategies almost always should be sensitive to population density and respond to reproductive rate, type of competition and equilibrium population size. As we want to analyse the influence of patch size on dispersal decisions we extend their model to allow for variance in patch capacities. In addition we add temporal fluctuations of demographic parameters to generate environmentally induced fluctuations in population size typical for many insect populations.

However, a shortcoming of the analysis of Travis et al. (1999) lies in their ad-hoc choice of a linear relationship between population density and dispersal probability. Thus, they restrict the outcome of their simulations to the given linear function, though they themselves suggest that a non-linear relationship might be more appropriate. To solve this problem we follow an approach recently presented by Metz and Gyllenberg (2001). Based on a fitness measure geared to a metapopulation, Metz and Gyllenberg present a general analytical approach to the evolution of dispersal in metapopulations and elegantly demonstrate the existence of a critical population density below which no individuals should disperse. We follow their marginal value type of argument but restrict our analysis to the specific case of non-overlapping generations with dispersal occurring during a short synchronised phase in the life cycle. Additionally, we are only interested in the derivation of a functional relationship between dispersal rate, population density, and patch size and leave explicit numerical calculations to simulation experiment. We are thus able to substantially simplify their analytical approach.

In this paper we will first present our analytical solution for the relationship between population density, patch size and ES-dispersal rates in a metapopulation with global dispersal. Our model is based on an ideal-free distribution approach (Doncaster 2000) and is very similar to the marginal value considerations presented by Metz and Gyllenberg (2001). The results of the analytical model will be tested by individual based simulation experiments. They allow us to investigate the quantitative influence of dispersal mortality and parameters affecting the population dynamics as well as that of simplifying assumptions in the analytical approach (e.g. global dispersal, neglect of kin-competition) on the evolution of dispersal rates.

2. An analytical model for the evolution of inter-patch dispersal

Consider a metapopulation of a number of habitat patches. Each of these patches supports a local population of a species which reproduces in distinct generations. In common with several other studies (e.g. Johst & Brandl 1997, Ruxton & Rohani 1998, Travis et al. 1999), we consider the case with generations split up into two distinct phases: reproduction and dispersal. All individual will take their decision to disperse or to stay simultaneously at the start of the dispersal phase. Individuals are allowed to disperse only once. This corresponds with Travis et al. (1999) and with the model of Metz

& Gyllenberg (2001) for the specific case of their s = 1. The assumption of a single dispersal event may be justified for many insects with non-overlapping generations and short periods suitable for dispersal.

We further assume that individuals can perceive and will base their dispersal decision on patch capacity (Ki) and pre-dispersal population density (Ci)

$$Ci = Ni/Ki$$
. with $Ni = actual population size in patch i$. (1)

Patch capacity will depend on both patch size and habitat quality. Throughout this paper we will assume that differences in patch capacity are only due to size (but see Metz & Gyllenberg 2001) and thus will use the term "patch size".

Each patch experiences a loss in density by emigration $(C_i \cdot d_i)$ and an increase in density by immigration (I_i/K_i) , with Ii the expected number of immigrants arriving in patch i. Density after dispersal is thus calculated as

$$C'_{i} = C_{i} - C_{i} \cdot d_{i} + \frac{I_{i}}{K_{i}} = C_{i} \cdot (1 - d_{i}) + \frac{I_{i}}{K_{i}}$$
(2)

The expected number of offspring for philopatric individuals (FP) in patch i depends on population density at the start of the reproductive phase, i.e. on density after dispersal ($^{F_{p}} = F_{p}(C'_{i})$). We assume logistic population growth. For all types of logistic growth the reproductive success of philopatric individuals (FP($^{C'_{i}}$)) will be a monotonously decreasing function of population density $^{C'_{i}}$.

We assume that a fraction (μ) of individuals will die before they reach another patch of suitable habitat. For the case of global dispersal all dispersing individuals are randomly distributed across patches Thus, all dispersing individuals face the same dispersal mortality (μ) and the expected reproductive success of dispersing individuals (FD) is independent of their natal patch (i). If we further assume size- and density-independent immigration, the mean number of immigrants per patch (I) will be constant and independent of patch identity. As a consequence, post-dispersal population density

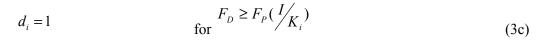
- (C') will always decrease and the reproductive success of philopatric individuals (FP($^{C'_i}$)) will increase with the fraction of individuals leaving a patch. Following the marginal value theorem (Charnov 1976) dispersal will be more profitable than philopatry as long as FD > FP(Ci'). For the calculation of patch specific equilibrium dispersal rates, di, we have thus to distinguish three possible situations:
- a) At very low population density, the expected success of philopatric individuals is greater than FD at any dispersal rate. In this situation it will be more profitable for all individuals to stay

$$d_{i} = 0 for F_{D} \le F_{P}(C_{i} + \frac{I}{K_{i}}) (3a)$$

b) With increasing population density individuals should disperse at a rate di equalizing the fitness of dispersing and philopatric individuals

$$0 \le d_i \le 1 \qquad \qquad for \qquad F_D \ge F_P(C_i + \frac{I}{K_i}) \tag{3b}$$

c) In some small patches the expected number of immigrating individuals (I) may already be sufficient to reduce post-dispersal fitness of philopatric individuals (FP) below the expected fitness of dispersing individuals (FD) regardless of dispersal rate. In this situation it will be more profitable for all individuals born in this patch to leave



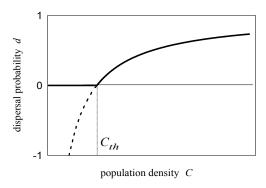


Figure 1 Predicted relationship (equation (3) and (4)) between population density C and dispersal probability d. With increasing density the function will asymptotically approach a probability of 1. Below the density threshold (C_{th}) , the function is confined to 0. An increase in patch capacity (K_i) will elevate C_{th} .

Since FD is independent of patch identity, $F_p(C_i')$ in patches satisfying condition (3b) must become independent of patch identity as well. This can either be realized in landscapes with constant population density (Parvinen 1999) or if the individual dispersal strategy (di) is sensitive to patch

density (Ci) and patch size (Ki) in such a way that post-dispersal population density (C_i) will become independent of patch identity as well

$$d_{i} = 1 - \frac{1}{C_{i}} (\hat{C} - \frac{I}{K_{i}}) \qquad \text{for } F_{p}(\frac{I}{K_{i}}) > F_{D} > F_{p}(C_{i} + \frac{I}{K_{i}})$$
(4)

where \hat{C} is the population density immediately after dispersal for which the reproductive success of dispersing individuals (FD) equals that of philopatric individuals in patches satisfying condition (3b), i.e.

$$F_D = F_P(\hat{C}) \tag{5}$$

We may now extract some predictions about the principal dispersal behavior following from equations (3) and (4).

(a) Individual dispersal probabilities should depend on population density Ci (except for very small patches; see condition (3c)). As long as population density inside a patch is less than the threshold density

$$C_{th} = \hat{C} - \frac{I}{K_i} \tag{6}$$

there will be no dispersal (Fig 1). We predict a nonlinear increase of dispersal probability di with population density Ci beyond this threshold density. According to equation (4), for all populations

satisfying condition (3b) dispersal will adjust post-dispersal density to \widehat{C} . Threshold density Cth is comparable to the threshold density \widetilde{x} in Metz & Gyllenberg (2001), and like these authors we expect a clumping of post-dispersal population densities around \widehat{C} .

- (b) Inspection of equation (6) makes clear that threshold density Cth declines with shrinking patch capacity Ki. Consequently, dispersal rates should increase with decreasing patch size (cf. McPeek & Holt 1992, Doncaster 2000) and reach unity in extremely small patches (condition 3c).
- (c) The influence of patch capacity (Ki) on threshold density (Cth) critically depends on the expected number of immigrants. (I). Consequently, the sensitivity of dispersal rates to patch size will depend on the two factors determining the number of immigrants, i.e. dispersal rate and dispersal mortality.
- (d) With increasing dispersal mortality (\square) fewer emigrating individuals will successfully reach a new habitat and the expected reproductive success of dispersing individuals declines. Hence, due to equation (5), FP must decrease, and \hat{C} increase as well. Since the number of immigrants I decreases, we can further conclude from equation (6) that threshold density Cth rises (and patch specific dispersal probability di declines) with increasing dispersal mortality.

An explicit numerical solution for the dispersal probability in a specific situation must be based on a calculation of \hat{C} and the number of immigrants I, which both depend on the population dynamics of the species studied. Only for the simple case of vanishing population fluctuations and consequently equal density in all patches we do not need an explicit expression for the expected number of offspring FP(Ci) to estimate \hat{C} and Ii (Parvinen 1999). However, for the case of logistic growth (or other models of density-dependent population growth) equation (4) will lead to an implicit formulation for dispersal rates. This makes it very difficult or even impossible to derive an analytical solution. We

models of density-dependent population growth) equation (4) will lead to an implicit formulation for dispersal rates. This makes it very difficult or even impossible to derive an analytical solution. We may thus either use an iterative approach as Parvinen (2001) has presented for the specific case of a species with continuous reproduction living in a metapopulation of indefinitely many equally-sized patches, or use Monte Carlo simulations like Travis et al. (1999). Additionally, simulation experiments allow us to evaluate the influence of some simplifying assumptions (like global dispersal or the neglect of kin competition) in our analytical approach. We thus used Monte Carlo simulations (i) to test the principal predictions of our analytical model, (ii) to quantify ES-dispersal rates in specific situations, and (iii) to analyze in more detail the relationship between dispersal mortality, the specific parameters relevant for population dynamics, and density dependent fitness on the one hand and ES-dispersal rates on the other.

3. Individual based simulation experiments

(a) The model

Our simulation experiments are based on an individual based model (i-state configuration model, cf. Caswell & John 1992) of insect dispersal in patchy landscapes. This model has successfully been used in studies of metapopulation dynamics in grasshoppers and butterflies (Poethke et al. 1996b, Poethke et al. 1999, Amler et al. 1999). The landscape simulated in our model consists of a number npatch of habitat patches of either constant or variable capacities Ki (see below).

Local population dynamics are governed by density-dependent reproduction of individuals according to a discrete-time logistic growth (Hassell 1998) that has successfully been fitted to the dynamics of numerous insect populations (Bellows 1981) and has also been used by Jánosi & Scheuring (1997) and Travis et al. (1999) in their model on the evolution of density-dependent dispersal. According to our model, a female gives birth to Λ offspring, where Λ is Poisson-distributed with mean $\Lambda_{mean}(t,patch)$. Insect populations show particularly large fluctuations in population size. These fluctuations result mostly from environmentally driven fluctuations in demographic parameters. We thus extend the model of Travis et al. (1999) and draw the patch-specific and time-dependent value of □mean(t,patch) from a lognormal distribution with mean λ and a standard deviation σ the latter determining the degree of environmental fluctuations. Environmental fluctuations are assumed to be uncorrelated in space and time. Offspring develop into mature individuals with a density-dependent survival probability s

$$s = \frac{1}{(1+aN_i)^{\beta}} \tag{7}$$

with

$$a = \frac{\lambda^{1/\beta} - 1}{K_i}$$

 β = density dependence;

Ni = population size in patch (i) at the start of the reproductive phase;

Ki = carrying capacity of patch i.

After all individuals have reached maturity, they disperse according to their individual dispersal probability d as outlined in the following paragraph.

Each individual is characterised by its sex, its affiliation with a specific patch i and by four alleles at two different diploid loci. The phenotype of individuals is determined by the arithmetic mean values

 p_C and p_K of the two corresponding alleles coding for density- (pC) and size-dependence (pK) of the individual's dispersal probability d. In agreement with equation (4) dispersal probabilities are calculated as

$$d = \begin{cases} 0 & \text{if} & C_i \leq C_{th} \\ 1 - \frac{1}{C_i} (\overline{p}_C - \frac{\overline{p}_K}{k_i}) & \text{if} & C_i > C_{th} & \text{and} & C_{th} > 0 \\ 1 & \text{if} & C_{th} \leq 0 \end{cases}$$

$$(8)$$

with ki = Ki/Kmean relative capacity of patch i;

Kmean = mean carrying capacity of patches in the landscape.

$$C_{th} = \overline{p}_C - \frac{\overline{p}_K}{k_i}$$
 patch-size dependent threshold density

Since pC is equivalent to C in equation (4) we expect pK to evolve towards the mean number of immigrants per patch (I).

In our model, individuals disperse before mating and production of offspring. Each individual has only one opportunity to disperse. Dispersing individuals die regardless of patch origin with a probability (μ) before they reach another suitable habitat. During the reproductive phase each female mates at random with one of the males present in the same patch (males can mate with several females). One corresponding allele for each locus of its descendants is then randomly drawn from each of its parents. However, any inherited parental allele can mutate with a probability m. In case of mutation, the corresponding value of pC or pK is modified by a value drawn with uniform probability from an interval between -0.1 and +0.1 (similar to Travis et al. 1999). To allow for greater variability of genotypes in the first generations and to reduce the influence of mutations on the stability of the final result, we performed all simulation experiments with decreasing mutation rates

$$m(t) = 0.1 \cdot e^{\frac{-2.5t}{t_{\text{max}}}} \tag{9}$$

with t = generation number

tmax = maximum number of generations.

Thus, independent of the simulated time, experiments started with mutation rates of approximately 0.1 and ended with rates below 0.001. Simulations are performed for three different scenarios:

Standard scenario. In this scenario all patches have the same capacity Ki = Kmean = 100. We assume global dispersal, i.e. dispersing individuals reach a patch with a probability of $(1-\mu)/(npatch)$. With uniform patch size the term pK in equation (10) becomes meaningless and is set to 0; only pC is free to evolve.

Variable-size. In this scenario, patch capacities are drawn from an even distribution (10 \le Ki \le 190) with mean capacity $K_{mean} = 100$. Equation (8) will be used to determine dispersal probabilities.

Nearest-neighbour: This scenario differs from the standard scenario by its dispersal mechanism. As Travis et al. (1999), we assume that individuals only disperse to the eight neighboring patches. To prevent edge effects we assumed our world to be a torus.

To get an impression of the influence of variation in model parameters on the evolutionarily stable dispersal rate d, we performed simulations with all possible combinations of the following parameter values: (i) mean reproductive rate (λ) = 2, 5, and 10, (ii) intra-specific competition (β) = 0.5, 2 and 10, (iii) dispersal mortality (μ) = 0.05, 0.10, 0.20, 0.40 and 0.80, and (iv) environmental variability (σ) = 0.0, 1.0, 1.5 and 2.0. This results in a total of 180 simulation experiments (3x3x5x·4) for each of the three scenarios.

(b) Results

Standard Scenario.

For all parameter combinations tested, mean dispersal rates dmean as well as the density coefficient of dispersal (pC) reached stable values after less then 3000 generations. We hence restricted simulation runs to 6000 generations, sufficient time to determine the evolutionary equilibrium. As shown in Figures 2 for some exemplary parameter combinations, threshold density (which is synonymous with pC in this scenario) as well as mean dispersal rate strongly depend on dispersal mortality and strength

of environmental fluctuations. While high dispersal mortality reduces mean dispersal rate due to an increase in threshold density, high environmental fluctuations have the opposite effect.

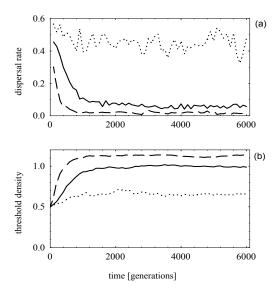


Figure 2 Evolution of (a) mean dispersal rate and (b) threshold density (C_{th}) in three different simulations (standard scenario) with variable values for dispersal mortality (μ) and environmental fluctuation (σ). Density-dependence ($\beta = 2.0$) and reproductive rate ($\lambda = 2.0$) were held constant. Full line: $\mu = 0.1$, $\sigma = 0.0$; dotted line $\mu = 0.1$, $\sigma = 2.0$; hatched line: $\mu = 0.4$, $\sigma = 0.0$.

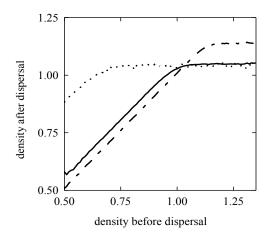


Figure 3 Mean population density after dispersal (C') as a function of density before dispersal (C). Mean values were taken over all patches and over the last 1000 generations of a simulation run. Parameters as in Figure 2. Full line: $\mu = 0.1$, $\sigma = 0.0$; dotted line $\mu = 0.1$, $\sigma = 2.0$; hatched line: $\mu = 0.4$, $\sigma = 0.0$.

Dispersal homogenizes post-dispersal population densities between patches (Figure 3). As long as population density remains below threshold density, no emigration occurs and post-dispersal population density is the sum of density before dispersal and the density increase due to immigration. As predicted by our analytical model, emigration reduces population density to a threshold density for patches with density above this threshold and post-dispersal density is thus similar in all of these patches.

A statistical analysis of the 180 standard simulations shows, that all four parameters varied in our simulation experiments (λ , β , σ , μ) have a significant influence on ES-dispersal rates and account for more than 95% of the variance in evolved dispersal rates (Table 1).

dependent variable: log ₁₀ (dispersal rate)	total $r^2 = 0.95$
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Source	d.f.	SS (Typ III)	F	p<	part r²- reduction	effect
constant term	1	233.86	16527.80	0.001		
β (density-dependence)	2	0.86	30.25	0.001	0.02	+
λ (pop.growth) * σ (env. var.)	11	19.57	83.7	0.001	0.37	$-(\lambda)$ $+(\sigma)$
μ (mortality)	4	30.08	531.48	0.001	0.57	-
error	162	2.29				

Table 1 Results of multivariate ANOVA on the relationship between evolved dispersal rate (\log_{10} -transformed) and rate of increase (λ), density-dependence (β), environmental variability (σ), and dispersal mortality (μ) for the standard scenario (180 simulation runs). Partial r²-reduction indicates the reduction in total uncorrected r² if term is removed from model, +/- in the last columns represent the direction of the relationship. For simplicity, weak effects ($r^2 < 0.01$) have not been included in the model.

ES-dispersal rates depend on the cost as well as the benefits of dispersal. As we do not include any investment costs of dispersal, cost of dispersal can completely be accounted for by dispersal mortality (μ) in our simulations. Excluding genetic aspects, the benefit of dispersal should be related to the amount of variation in population density which is relevant for the potential fitness improvement due to dispersal. A statistical model replacing the explanatory variables presented in Table 1 by dispersal mortality and the log10-transformed coefficient of variation in population density between patches (CVpd) can explain equally well the variance in the observed dispersal rates (ANCOVA F=610.5, p<0.001, r²=0.97 including a highly significant interaction term between dispersal mortality and CVpd: F=337.3, p<0.001) An analysis of the remaining residual variation demonstrates that the influence of the reproductive rate (λ)and environmental fluctuations (σ) on dispersal rates are nearly completely accounted for by their effect on CVpd (cf. Figure 4); they explain only 0.09 of the remaining small variance in dispersal rates (ANOVA part. F=3.20, d.f.=11, p<0.01).

According to our analytical model, dispersal rates should decrease and threshold density increase with increasing dispersal mortality. Figure 5a and 5b (compare separate lines) prove that both predictions are met in our simulations. As already mentioned above, we also see a positive relationship between the CVpd and observed dispersal rates (Figure 5a). However, as a given threshold density is more often reached at higher CVpd, an increase in CVpd automatically results in higher mean dispersal rates. Thus, there is no simple relationship between the threshold density and the CVpd (Fig. 5b), at least at high dispersal mortality.

As evident from table 1, density-dependence (β has only a small positive influence on dispersal rates: β accounts for approximately $\frac{1}{2}$ of the variation in dispersal rate after accounting for the effects of dispersal mortality and CVpd (ANOVA part. F=87.46, d.f.=2, p<0.001, r²=0.46), with dispersal rates significantly lower at β = 0.5 compared to β = 2 or 5. Obviously dispersal mortality defines the cost of dispersal. However, the benefit of dispersal is a function of both, the expected magnitude in density-

reduction by emigrating from a patch with high density (dependent on CVpd) and the fitness consequences of this improvement. The latter is determined by density-dependence (β) .

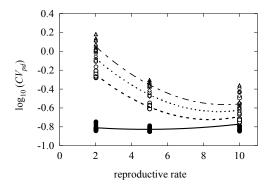


Figure 4 The effect of environmental variation (σ) and mean reproductive rate (λ) at variable density-dependence (β) on the \log_{10} -transformed coefficient of variation in population density (CV_{pd}). Ψ and solid line $\sigma = 0.0$; Ψ and hatched line $\sigma = 1.0$; Ψ and dotted line $\sigma = 1.5$; ∇ and long-hatched line $\sigma = 2.0$.

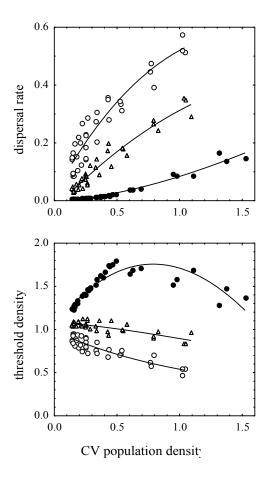


Figure 5 Population mean dispersal rate and mean threshold density C_{th} ($\hat{=}$ p_C) as functions of dispersal mortality (μ) and coefficient of variation in population density (CV_{pd}). Results of 36 replicate simulation experiments for each of the following values for mortality: $\mu = 0.05$ (Ψ); $\mu = 0.2$ (∇); $\mu = 0.8$ (Ψ). σ , λ , and β variable across simulation experiments.

Comparison between scenarios.

Results of the "variable-size" and "nearest-neighbour" scenario are very similar to those of the standard scenario. The difference between scenarios in the relationship between CVpd and realized dispersal rates is hardly recognizable and not statistically significant. As a limitation of dispersal to adjoining patches will principally increase the amount of kin-competition after dispersal (cf. Gandon & Michalakis 1999, Gandon & Rousset 1999, Plantegenest & Kindlmann 2000, Irwin & Taylor 2000), the similarity in dispersal rates between the standard and nearest-neighbor scenario seems to contradict the relevance of kin-competition for the evolution of dispersal. However, in the variable-size scenario, we find a significant deviation of the size-coefficient from its expected value (Figure 6), i.e. the sensitivity to patch-capacity is larger than predicted by our analytical model. According to equation (8) this especially affects dispersal from small patches. As mean dispersal rates were not altered by the introduction of variable patch sizes, this elevated size-factor may indicate an effect of kin-competition on dispersal strategies. This assumption is further supported by an analysis of mean offspring numbers for dispersing and philopatric individuals. In contrast to the assumptions in our analytical model and in other models ignoring kin competition (e.g. Ronce et al. 2000b, Metz & Gyllenberg 2001, Parvinen 2001), the mean number of offspring for dispersing individuals (FD) is smaller than that for individuals that stay in their natal patch (FP). This difference strongly depends on mean dispersal rates. While it is smaller then 1% for high dispersal rates (d > 0.2) it may increase to more then 30 % in the case of extremely small dispersal rates (d < 0.02).

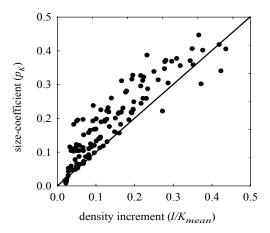


Figure 6 Relationship between evolved size coefficient (p_K) and observed mean density increase due to immigration (for patches with mean capacity) in 180 simulations with variable patch capacity ("variable size" scenario). According to equations (4) and (8) points are expected to fall on the main diagonal. σ , λ , and β variable across simulation experiments.

4. Discussion

In our paper, we combine the simulation approach of Travis et al. (1999) with an analytical model similar to that of Metz & Gyllenberg (2001). While we use the analytical approach to derive the qualitative (nonlinear) relationship between population density and dispersal rate, the simulation experiments help to test the results of this analysis and extend them to quantitative predictions. We

thus combine the explanatory strength of analytical models with the greater flexibility of simulation experiments.

In our analytical approach we did not define a specific relationship between population density and fitness leaving the investigation of specific predictions for a given population growth model (i.e. fitness function) to the simulation experiments. We thus get around many of the restrictions used in other purely analytical models, e.g. an extremely reduced strategy set (Paradis 1998), either an infinite number of populations (Gandon & Michalakis 1999) or only two (McPeek & Holt 1992, Doebeli & Ruxton 1997), the allowance of only two population states (Gandon & Michalakis 1999), limitation to global (Metz & Gyllenberg 2001) or nearest neighbor dispersal (Jánosi & Scheuring 1997, Ruxton & Rohani 1998, Travis et al. 1999, Irwin & Taylor 2000), the assumption of cost-free dispersal (McPeek & Holt 1992, Lebreton et al. 2000, Mathias et al. 2001), and the requirement for either extremely small (Ezoe & Iwasa 1997, Irwin & Taylor 2000) or infinite population size (Metz & Gyllenberg 2001).

With our model, we extend the problem posed by Olivieri & Gouyon (1997) to patch-size dependent dispersal. We derived a nonlinear expression for the ES conditional dispersal strategy assuming that individuals can perceive both, the local population density and patch size (capacity). In good agreement with previous results (e.g. Jánosi & Scheuring 1997, Ruxton & Rohani 1998, Travis et al. 1999, Metz & Gyllenberg 2001) our model predicts that individuals should only disperse from patches with local population density above a certain threshold and that dispersal tends to homogenize population density across patches above this threshold (cf. Ruxton & Rohani 1998, Metz & Gyllenberg 2001).

Recently, Kindvall & Petersson (2000) have demonstrated that size-dependent migration can have substantial effects on predicted metapopulation extinction rates. However, as population level (extinction risk) and individual level (fitness) considerations may lead to quite different predictions concerning optimal dispersal strategies (Comins et al. 1980), it is reassuring to find a positive fitness-effect of size-dependent dispersal as well. For the special case of no dispersal costs and two-patches, this has already been predicted by McPeek & Holt (1992). Their model is the specific realization of our more general approach for these restricted conditions. Our analytical model (equation 6b) also shows that the fitness relevance of size-dependent dispersal would disappear if immigration were directly proportional to patch capacity (cf. McPeek & Holt 1992). In real systems, some intermediate form of size-dependence may occur, e.g. with emigration proportional to patch size (area) and immigration proportional to patch perimeter (Kindvall & Petersson 2000).

In particular in small populations and for small dispersal rates, kin competition may strongly influence dispersal rates (e.g. Hamilton & May 1977, Gandon & Michalakis 1999, Gandon & Rousset 1999, Irwin & Taylor 2000, Ronce et al. 2000a). Like most demographic models (e.g. Parvinen 1999, Ronce et al. 2000b, Metz & Gyllenberg (2001) our analytical model ignores this effect and eventually underestimates the sensitivity of dispersal probability to patch capacity. As individual-based models account for kin competition, this may explain the small discrepancy between the magnitude in the size coefficient predicted by the model (equation 4 and 8) and the values realized in our experiments (Fig. 7). This interpretation is also supported by the observation that offspring production of dispersing individuals was substantially lower than that of philopatric individuals only when overall dispersal rate was low. Under this condition, relatedness of individuals within patches will be high and costs of dispersal can be accounted for by the benefits given to philopatric relatives. This is in good agreement with predictions from kin selection models, which predict an increase in dispersal with increasing relatedness in local patches (e.g. Taylor 1988, Ronce et al. 2000a). Thus, we suggest that - when local populations are small and dispersal is rare - models which ignore inclusive-fitness considerations may

underestimate ES-dispersal rates. Further simulation experiments with smaller patch sizes, modified dispersal models, and a thorough analysis of relatedness in local populations (Poethke & Hovestadt in prep.) should allow to quantify the influence of kin competition in relation to demographic effects.

Of practical relevance may be the fact that the evolved dispersal rate can be accounted for by dispersal mortality and the coefficient of variation in population density only. A detailed knowledge of population parameters is thus not required to predict dispersal rates. This will ease the validation of our predictions by field experiments and allows to extend the predictions drawn from our simulation experiments. For example, in the simulation experiments environmental fluctuations were assumed to be uncorrelated in space and time. However, with spatially correlated fluctuations and limited dispersal distance, the variation in population density between the home patch and potential target patches will be reduced. In this case, evolution may lead to both, a reduction in dispersal rates and an increase in dispersal distance.

For the logistic growth model used in our simulations, the coefficient of variation mainly depends on reproductive rate (λ) and environmental fluctuations (σ). The additional effect of density-dependence (β) on evolved dispersal rate is comparably small. This may be surprising and differs from the findings of Travis et al. (1999) and Johst et al. (1999). We ran additional simulations (Poethke) implementing the model for population growth suggested by Maynard Smith & Slatkin (1973) and used by Ruxton & Rohani (1998) and Johst et al. (1999). However, they did not demonstrate a stronger influence of β on dispersal rate as long as parameter combinations did not result in chaotic local population dynamics (combinations of high β and high λ).

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